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This technical report has been reviewed and is approved for publication.

EMERY D. LEFLER, Chief Integration Division

Directorate of Design Analysis
Daputy for Development Planning

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FOREWORD

The purpose of this work was to establish a method to predict aircraft inertia suitable to preliminary design. It must be applicable to all types of military aircraft and be usable with the level of information normally available during preliminary design.

The material in this report was compiled as a part of the continuing methods development effort under project AFSD00370000N, Flying Qualities Methodology and Development. The effort was accomplished within ASD/XRHI by Charles Lanham while a cooperative student under the direction of Wayne M. O'Connor.

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TABLE OF CONTENTS

Secti	<u>lon</u>	Page
ı.	INTRODUCTION	1
II.	BACKGROUND	2
	A. Basic Moment of Inertia Theory	2
	B. Method Description	3
	C. Weight Allocation	4
III.	GROUP INERTIAS AND TOTALS	5
	A. Surfaces	6
	B. Fuselage	9
	C. Propulsion	13
	D. Internal Fuel	14
	E. Payload	16
	F. Additional Items	17
	G. Total Aircraft Inertias	18
IV.	SAMPLE PROBLEM: C-5A	20
4 17	131114175 7 14	

APPENDIX

REFERENCES

LIST OF SYMBOLS

TERM	DEFINITION
b ₁	span of surface panel from root chord to tip*
^b 2	span of surface panel from root chord to break*
^b 3	span of surface panel from break chord to tip
b ₄	span of wing fuel tank
^c r	length of surface root chord*
CREWCg	perpendicular distance from YZ plane of the remote axes to the crew center of gravity.
c ₂	length of surface chord at break
c ₃	length of most inboard chord for wing fuel tank
d _p	average diameter of payload
I	mement of inertia of a group or component about the remote axes
Icg	moment of inertia of total aircraft about its own center of gravity
Io	moment of inertia of a group or component about its own center of gravity
1	moment of inertia of a surface about the leading edge of the root chord or break chord*
14	moment of inertia of a fuel tank about the leading edge of the most inboard tank chord
1 _e	length of fuselage center section
1 _e	length of nacelle (for buried engines just length of engine)
$^{1}\mathbf{f}$	longitudinal length of fuselage tank
1 _n	length of fuselage nose cone
1 _p	length of fusciage tail cone
1 _v	length of item used as a volume in fuselage

TERM	DEFINITION
R	average fuselage radius ($\frac{Smax}{\pi}$)
R _e	average nacelle radius (for buried engines use radius of engine)
R _V	average radius of item used as a volume in fuselage
s _c	wetted area of fuselage center section
s_1	external store or tank length
Sn	wetted area of fuselage nose come
s _r	average radius of external tank or store
s _t	wetted area of fuselage tail cone
t _b	thickness of surface at break chord $(\frac{t}{c} \cdot c) \star$
^t f	thickness of wing fuel tank at most inboard chord
t _o	thickness of wing fuel tank at most outboard chord
t _r	thickness of surface at root chord ($\frac{t}{c}$ · c)
t	thickness of surface at tip chord ($\frac{\mathbf{t}}{\mathbf{c}} \cdot \mathbf{c}$)
W _C	weight of fuselage center section (structure only)
w _{dc}	total weight of contents to be distributed throughout the fuselage
We	total propulsion group weight divided by the number of engines
Wff	weight of fuel in the fuselage
Wfw	weight of fuel in both wing fuel tanks
w _h	weight of total horizontal tail group
Wi	weight of both surface inboard of break
W _n	weight of fuselage nose cone (structure only)

TERM	DEFINITION
Wo	weight of both surfaces outboard of break
W _p	weight of one point mass
W _{Pc}	total weight of point masses in the fuselage center section
Wpnc	total weight of point masses in nose and tail cones
Ws	weight of fuselage structure
W _{st}	weight of external fuel tank or store
W _E	weight of fuselage tail cone (structure only)
Wv	weight of total vertical tail group
Wvo	weight of one volume of mass
W	weight of total wing group
XF1	distance from the wing fuel tank leading edge at most inboard tank chord to the longitudinal tank center of gravity
XF2	perpendicular distance from YZ plane of the remote axes to leading edge of wing fuel tank most inboard chord
XP	perpendicular distance from YZ plane of the remote axes to engine center of gravity
XS1	distance from the surface leading edge at root chord to the longitudinal surface center of gravity
XS2	(surface with leading and/or trailing edge break) distance from the surface leading edge of root chord to the longitudinal center of gravity for the surface section inboard of the break. *
XS3	(surface with leading and/or trailing edge break) distance from the surface leading edge break chord to the longitudinal center of gravity for the surface section outboard of the break.
XS4	perpendicular distance from YZ plane of the remote axes to leading edge of surface root chord
XS5	perpendicular distance from YZ plane of the remote axes to leading edge of surface break chord viii

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TERM	DEFINITION
χ	perpendicular distance from Z axis to aircraft center of gravity
$\bar{\bar{\mathbf{x}}}$	distance from a defined reference point to the surface longitudinal center of gravity
YF1	distance from the wing fuel tank most inboard chord to the spanwise tank center of gravity
YF1	perpendicular distance from the XZ plane of wing fuel tanks most inboard chord to the spanwise tank center of gravity. (YF1 $\cos \theta$)
YF2	perpendicular distance from XZ plane of the remote axes to most inboard chord of wing fuel tank
YP	perpendicular distance from XZ plane of the remote axes to engine center of gravity
YS1	distance along span of surface from root chord to center of gravity
YŠ1	perpendicular distance from XZ plane of surface root chord to spanwise center of gravity (YS1 cos $\boldsymbol{\theta}$)
YS2	distance along span of surface from root chord to center of gravity for inboard surface
Y\$2	perpendicular distance from XA plane of surface root chord to spanwise center of gravity for inboard surfaces. (YS2 cos 0)
YS3	distance along span of surface from break chord to center of gravity for outboard surface
YŠ3	perpendicular distance from XA plane if surface break chord to spanwise center of gravity for outboard surfaces (YS3 cos 0)
YS4	perpendicular distance from XZ plane of the remote axes to the surface root chord
Ÿ	distance from some reference point a surface spanwise center of gravity
z _b	perpendicular distance from XY plane of the remote axes to fuselage centerline

TERM	DEFINITION
ZF	perpendicular distance from XY plane of the remote axes to wing fuel at most inboard chord
ZF2	(YF1 $\sin \theta$) (needed only for wing internal tanks with anhedral or dihedral) perpendicular distance from the XY plane of the surface root chord to the vertical center of gravity
ZP	perpendicular distance from XY plane of the remote axes to engine center of gravity
ZS1	perpendicular distance from XY plane of the remote axes to root chord of surface
Z\$3	(YS1 sin θ) perpendicular distance from the XY plane of the surface root chord to the vertical surface center of gravity. *
2 \$4	(YS2 sin θ) perpendicular distance from the XY plane of the surface root chord to the vertical center of gravity of the surface panel inboard of the break. $*$
zss	(YS3 $\sin \theta$) perpendicular distance from the XY plane of the surface break chord to the vertical center of gravity of surface panel outboard of the break
Ž	perpendicular distance from X axes to aircraft center of gravity
Z Z	distance from some reference point to a vertical surface center of gravity

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TERM	DEFINITION			
ZF	perpendicular distance from XY plane of the remote axes to wing fuel at most inboard chord			
ZF2	(YF1 $\sin \theta$) (needed only for wing internal tanks with anhedral or dihedral) perpendicular distance from the XY plane of the surface root chord to the vertical center of gravity			
ZP	perpendicular distance from XY plane of the remote axes to engine center of gravity			
ZS1	perpendicular distance from XY plane of the remote axes to root chord of surface			
253	(YS1 sin θ) perpendicular distance from the XY plane of the surface root chord to the vertical surface center of gravity. *			
ZS4	(YS2 sin θ) perpendicular distance from the XY plane of the surface root chord to the vertical center of gravity of the surface panel inboard of the break. *			
285	(YS3 sin θ) perpendicular distance from the XY plane of the surface break chord to the vertical center of gravity of surface panel outboard of the break			
ž	perpendicular distance from X axes to aircraft center of gravity			
Ž	distance from some reference point to a vertical surface center of gravity			

TERM	DEFINITION
$^{\Lambda}_{ extbf{L1}}$	sweep of surface leading edge at root
^ La	sweep of surface leading edge outboard of break
^ _{T1}	<pre>sweep of surface trailing edge at root *</pre>
$^{\Lambda}_{ m T2}$	sweep of surface trailing edge outboard of break
$^{\Lambda}_{L3}$	sweep of wing fuel tank leading edge
$^{\Lambda}_{\mathbf{T3}}$	sweep of wing fuel tank trailing edge
ρ	density of fuel
θ	angle in degrees between plane of surface and XY plane of remote axes (positive for dihedral, negative for anhedral)
*	root chord can be defined as either theoretical or exposed
(see section II A	()

SECTION I

INTRODUCTION

The purpose of this procedure is to determine the inertias of an aircraft at the preliminary design level so that the dynamic performance (flying qualities) can be examined. The purpose of analyzing dynamic performance at the preliminary design level is to insure adequate control surface sizing, develop control surface sizing rules for parametric design studies, and to determine the complexity of the flight control system necessary to adequately perform all required maneuvers. To do this, the procedure must be able to provide reasonably accurate estimates for different fuel and loading states.

The method described in this report has been incorporated into the ASD/XR Interactive Computer Design (ICAD) system. The flying qualities analysis portion of this system is described in Reference 1.

SECTION II

BACKGROUND

A. Basic Moment-of-Inertia Theory

Moment of inertia is the measure of resistance to angular acceleration, as mass is the measure of resistance to linear acceleration.

Moment of inertia may be mathematically derived as follows.

If torque is expressed as the product of force and radius (T = Fr) and the following substitutions are made: F = ma and $a = \alpha r$ then T = mar or $T = mr^2 \alpha$ where a is the linear acceleration, α is the angular acceleration, and m is the mass.

The term mr^2 is defined as the moment of inertia (I) and this equation may be written $T = I\alpha$.

If a body of mass m is caused to rotate about a remote axis y the following relationship exists: $I_y = mr^2 = m(x^2 + z^2)$.

However, since mass m not only offers resistance to rotation about the y axis but also offers resistance to rotation about its own centroidal axis, the total inertia of m about y is $I_y = mr^2 + I_{oy}$ where I_{oy} is the inertia of m about its own centroidal axis.

When the full angular momentum equations are developed, there are nine I_0 terms given in general by: $I_{0} = \int_{x_i x_j} x_j dm$ where x_i, x_j , can be x, y, or z. Since the symmetric erms are equal, e.g., $I_{0} = I_{0}$, there are actually six independent moments of inertia.

For most aircraft problems, the vehicle is symmetric about the XZ plane. Although there are asymmetries in equipment locations which give rise to some non-zero values, it can be assumed for preliminary design purposes that I_{xy} and I_{yz} are zero. There are some configurations where this assumption obviously is not correct, such as skewed wings. For these aircraft the additional terms should be calculated. This method is limited to predicting the four remaining moments of inertia, I_{x} , I_{y} , I_{z} , and I_{xz} .

B. Method Description

There are three steps involved in obtaining these moments of inertia:

- 1) Allocate the total aircraft weight to six seperate groups:
 - a. wing group
 - b. horizontal tail group
 - c. vertical tail group
 - d. fuselage group
 - e. propulsion group
 - f. additional items

The level of detail of the weight breakdown given in Table 9 of Section II is adequate for determining the inertias. This allocation primarily involves distributing the subsystems throughout the aircraft without identifying the actual location of each wire, cable, line, or component. Since this is done on an "historical" or "accepted design practice" basis, adjustments may be needed for designs with unusual concepts or distributions.

- 2) Calculate the moment of inertia of each group about its own centroid and then transfer these inertias to a set of remote axes.
- 3) Locate the aircraft center of gravity, sum the inertias, and translate them back to the aircraft center of gravity to obtain the desired moments of inertia. The last two steps are described in detail in Section III.

2

C. Weight Allocation

Allocation of the total aircraft weight to the major groups is accomplished by a apckage of rules extracted from a structural weight estimation program (SWEEP) written by Rockwell International and from statistical data. The aircraft items are distributed as shown in Table 1.

TABLE 1
WEIGHT ALLOCATION

	Fraction in Fuselage	Fraction in Wing	Fraction Horiz Tail	Fraction Vert Tail	Fraction With Engine Package	Fraction With Items
Horiz tail						
structure	_	_	1.0		_	_
Vertical tail	ł i		1.0	ľ		
structure	_	_	_	1.0	-	_
Fuselage struc-	.i]	
ture	1.0	-	_	- 1	_ [_
Main gear	1	D	D	-	-	_
Nose gear	1.0	- 1	_	- 1	-	-
Engine Nacelle	1					
& Pylons	-	-	-	-	1.0	-
Other structure	1.0	-	-	-	-	-
Engine	-	- 1	-	-	1.0	-
Aux gearboxes	-	-	-	-	1.0	-
Exhaust system	-	-	-	-	1.0	-
Cooling & drain		-	-	-	1.0	-
Lubricating sys		-	- 1	-	1.0	-
Engine controls	-	- 1	-]	-	1.0	-
Starting sys	-	-	- }	-	1.0	-
Auxiliar power unit	1.0	-	-	-	-	-
Instruments	1.0	-	- }	-]	-	-
Hydraulics	0.67	-	- }	-	0.33	-
Electrical	0.75	-	-	- 1	0.25	-
Electronics	1.0	-	-	-]	-)	-
Armament	1.0	-	-	-	-	-
Air conditionin		- [-	- 1	- 1	-
Photographic	1.0	-	- j	- }	-	-
Auxiliary gear	1.0	-	- 1	-	-	-
Other equipment		-	- 1	-	-	-
Crew	1.0	-	- }	-	-	-
011	-	-	-	-	1.0	-
Liquid Nitrogen		-]	-	-	-	-
Miscellaneous	1.0	l	į	!		
Payload	-	-	- i	-	-	1.0
Guns	j - j	-	-	- j	- }	1.0
		'	1	•	ſ	l

Table 1 Cont'd

THE PARTY OF THE P

]				
Wing Pylons	~	<u>-</u> ,	-	-	-	1.0
Ext Wing tanks	-	-	-	-		1.0
fuselage pylons	-	-	-	-	_	1.0
Ext Fus tanks	-	-	_	-	-	1.0
Fuel	-		-	-	-	1.0
						<u> </u>

Note D = dependent on input location definition.

Items which need further discussion:

- a. Fuel System Distribute between the fuselage and wing group according to the fraction of fuel weight contained in each group.
 - b. Surface Controls: Summarized in table:

Table 2
SURFACE CONTROL WEIGHT ALLOCATION

Fraction of Total Surface Control Weight					
Configuration Code W, H, V*	Wing	Horizontal Tail	Vertical Tail	Fuselage Cockpit	Fuselage Distributed
0, 0, 0	0.532	0.128	0.124	0.038	0.178
0, 0, 1	0.457	0.110	0.247	0.033	0.153
0, 1, 0	0.464	0.239	0.108	0.034	0.155
0, 1, 1	0.406	0.209	0.220	0.029	0.136
1, 0, 0	0.608	0.108	0.103	0.032	0.149
1, 1, 0	0.541	0.205	0.092	0.029	0.133
1, 0, 1	0.534	0.094	0.213	0.028	0.131
1, 1, 1	0.482	0.182	0.192	0.026	0.118

*W, wing
H, horizontal

0 = fixed

1 = variable sweep

V, vertical tail

0 = elevator type
0 = rudder type

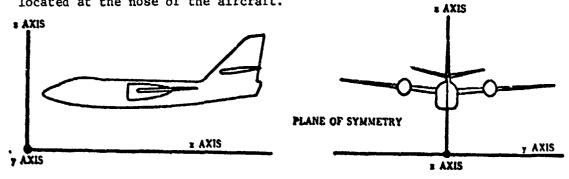
1 = all moveable type
1 = all moveable type

- c. Trapped fuel Distribute between fuselage and wing group according to fraction of fuel weight contained in each group.
- d. Air induction system Add weight to fuselage group if engines are buried. Add to engine group if engines are podded.
- e. Wing structure If there is a wing carry-through structure, the weight should be added to the wing group Otherwise only the exposed wing structure is in the wing group.

SECTION III

GROUP INERTIAS

Before the centroidal inertias (I 's) of each group can be calculated and then translated to the remote set of axes, a certain amount of component location and geometry information must be known. Everything should be referenced in accordance with the chosen set of remote axes (see sketch). The exact position of these axes can be varied, but to make the calculations easiest, the Z axis should be located at the nose of the aircraft.



Below is a list of additional components whose X, Y, and Z locations have to be determined if they are to be included. All geometry information that is needed is included with the discussion of each major group.

- 1) Main and nose landing gear
- 2) Auxiliary power unit
- 3) Air conditioning
- 4) Auxiliary gear
- Gun

- 6) Crew
- 7) Weapons
- 8) Fuel system (Centroid of fuselage fuel tank)
- 9) Avionics bays
- 10) Radar

- 11) Furnishings & Equipment (centroid of total group or centroids of major items)
- 12) Photographic equipment
- 13) Other equipment
- 14) Liquid nitrogen
- 15) Miscellaneous items
- 16) Fuselage store and tank pylons
- 17) Fuselage external stores and tanks
- 18) Wing store and tank pylons
- 19) Wing external stores and tanks
- 20) Internal Payload

Using this information we can now proceed to calculate the moments of inertia of the separate groups about their own centroidal axes and translate these to the remote axes.

A. Surfaces

Wing, horizontal tail, and vertical tail groups are all common surfaces. To define the shape of the surface the normal planview (one side of wing and horizontal since they're symmetrical) is used. The equations are derived for a trapezoidal panel with the thickness varying linearly from root to tip. If a surface has edge or thickness breaks, it should be separated into inner and outer trapezoidal panels with the inertia of each calculated separately. The thickness is assumed constant as you go from leading to trailing edge and equal to the maximum for that section.

$$I_{1x} = \frac{Wb^{3}}{V} \left\{ \left[(t_{r} - t_{i}) \left(\frac{c}{4} + \frac{b \tan \Lambda_{T}}{5} - \frac{b \tan \Lambda_{L}}{5} \right) \right] + \left[t_{r} \left(\frac{c}{3} + \frac{b \tan \Lambda_{T}}{4} - \frac{b \tan \Lambda_{L}}{4} \right) \right] \right\}$$

$$I_{1y} = \frac{Wb}{V} \left\{ \left[t_{r} \left(\frac{c^{3}}{3} + b \cot n \Lambda_{T} \left(\frac{c}{2} + \frac{b \tan \Lambda_{T}}{3} \right) + \frac{b^{3}}{12} (\tan^{3} \Lambda_{T} - \tan^{3} \Lambda_{L}) \right] - \left[(t_{r} - t_{t}) \left(\frac{c^{3}}{6} + b \cot n \Lambda_{T} \left(\frac{c}{3} + \frac{b \tan \Lambda_{T}}{4} \right) + \frac{b^{3}}{15} (\tan^{3} \Lambda_{T} - \tan^{3} \Lambda_{L}) \right] \right\}$$

$$(2)$$

$$I_{iz} = I_{ix} + I_{iy} \tag{3}$$

$$V = b \left\{ t_r \left[c + \frac{b}{2} \left(tan \Lambda_r - tan \Lambda_L \right) \right] - \left(t_r - t_L \right) \left[\frac{c}{2} + \frac{b}{3} \left(tan \Lambda_r - tan \Lambda_L \right) \right] \right\}$$
(4)

The inertia equations for this volumetric shape are derived (see Appendix Section 1) with the assumption that all surfaces lie in planes parallel to the XY plane of the remote axes.

To take into account the fact that surfaces don't always lie in planes parallel to the XY plane but usually have some anhedral or dihedral:

True
$$I_{1y} = (I_{1y} \cos \theta + I_{1z} \sin \theta)$$
 (5)

True
$$I_{1z} = (I_{1y} \sin \theta + I_{1z} \cos \theta)$$
 (6)

I, is not affected by dihedral.

The product of inertia I_{1xz} is non-zero only if there is some dihedral or anhedral.

$$I_{1x2} = \bigvee_{V} t_{r} \sin \Theta \left[\frac{c_{r}^{2}b^{2}}{4} + \frac{c_{r}^{2}b^{3}}{3} t an \Lambda_{T} + \frac{b^{4}}{8} \left(t an^{2} \Lambda_{T} - t an^{2} \Lambda_{L} \right) \right] - \bigvee_{V} \left(t_{r} - t_{e} \right) \sin \Theta \left[\frac{c_{r}^{2}b^{3}}{6} + \frac{c_{r}^{2}b^{3}}{4} \right]$$

$$tan \Lambda_{T} + \frac{b^{4}}{10} \left(t an^{2} \Lambda_{T} - t an^{2} \Lambda_{L} \right) \right]$$

$$(7)$$

These equations calculate the inertias for the entire wing, horizontal, or vertical tail as long as the total group is used.

If a wing does not have a carry-through structure, the exposed wing should be used and the symbols should be defined accordingly. Otherwise, a theoretical wing should be used. All horizontal and vertical tails should be defined with exposed parameters. The equations shown here calculate the inertias for the entire inboard or out-board surfaces (left and right) as long as the total weight for each was used and the symbols were defined correctly.

Table 3 shows how to define the general symbols used in all equations dealing with surfaces, for each separate surface.

Table 3. Surface Symbols

Before I_1 can be translated back to obtain the surface I_0 , the centroids of the surfaces must be known. All longitudinal surface centroids can be found by a method from DATCOM (See Appendix Section 2) as long as the parameters c, b, and A_1 are again properly defined for each surface.

Table 3. Surface Symbols

GENERAL SYMBOL		DEFINED SYMBOLS		
	WING (NO BREAK)	INBOARD SURFACE	OUTBOARD SURFACE	HORIZ. & VERT.
Λ _L	Λ _{L1}	^A L1	۸ L2	^L1
ΛŢ	^ _{Tl}	^ Tl	^A T2	Λ _{T2}
b	b 1	b ₂	b ₃	b 1
С	c _r	e _r	c ₂	c ₁
^t r	^t r	t _r	t _b	t _r
^{t.} t	t	t _b	tt	t
W	w _w	$w_{\mathtt{i}}$	Wo	$\mathbf{w_h}, \mathbf{w_v}$
$\bar{\bar{\mathbf{x}}}$	XS1	XS2	XS3	XS1
Ÿ	Y\$1*	Y\$2*	Y\$3	Y\$1**
ž	ZS3***	ZS4***	ZS5***	Z\$3***

^{*} If YS4 = 0 and 0 = 0 Set these = 0.

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Before I_1 can be translated back to obtain the surface I_0 , the centroids of the surfaces must be known. All longitudinal surface centroids can be found by a method from DATCOM (See Appendix, Section 2) as long as the parameters c, b, and Λ_L are again properly defined for each surface.

$$xs1, xs2, xs3 = (-c_a^2 + c_b^2 + c_c c_b + c_c^2) \sqrt{(\kappa_o)}$$

$$3 (c_b + c_c - c_a)$$
(8)

where C_a is the smallest of the following values: c, b tank , b tank L + c C_b is the intermediate value; C_c is the largest value

 $K_0 = .703$ for a wing

 $K_0 = .771$ for horizontal or vertical tail

^{**} If YS4 = 0 and 0 = 0 Set these = 0.

^{***} Not needed if 0 = 0.

All spanwise surface centroids are assumed to be at the spanwise surface center of volume. These centroids are needed only for exposed wing surfaces, outboard surfaces and for vertical tails since these all have inertias that need to be translated (see Appendix, Section 2).

YS1, YS2, YS3 =
$$\frac{b^2}{V}$$
 [(t_r ($\frac{c}{2} + \frac{b}{3}$ ($tan\Lambda_T$ - $tan\Lambda_L$)) - (t_r - t_t) $\frac{c}{3} + \frac{b}{4}$ (9) ($tan\Lambda_T$ - $tan\Lambda_L$))]

All vertical center of gravity distances for surfaces with $\theta=0$ are negligible because of the small thickness of surfaces compared with their length and span. For surfaces with either anhedral or dihedral the vertical center of gravity (\overline{z}) no longer lies in the XY plane of the root or break chord and can be calculated by:

$$ZS3 = YS1 \sin \theta \tag{10}$$

$$ZS4 = YS2 \sin \theta \tag{11}$$

$$ZS5 = YS3 \sin \theta \tag{12}$$

With the surface centroid location known, I can be translated to the centroid and then to the remote axes. For wings (no break), horizontal, and vertical surfaces, the I values are calculated by:

$$I_x = I_{1x} - w(Y\dot{S}1)^2 - w(ZS3)^2 + w(Y\dot{S}1 + YS4)^2 + w(ZS3 + ZS1)^2$$
 (13)

$$I_y = I_{1y} - w(xs1)^2 - w(zs3)^2 + w(xs1 + xs4)^2 + w(zs3 + zs1)^2$$
 (14)

$$I_z = I_{1z} - w(xs1^2 + ys1^2) + w(xs1 + xs4)^2 + w(ys1 + ys4)^2$$
 (15)

$$I_{xz} = I_{1xz} - W(XS1) (ZS3) + W(XS1 + XS4) (ZS3 + ZS1)$$
 (16)

For inboard surfaces:

$$I_x = I_{1x} - w(\dot{y}\dot{s}\dot{z}^2 + z\dot{s}\dot{z}^4) + w(z\dot{s}\dot{z} + z\dot{s}\dot{z})^2 + w(\dot{y}\dot{s}\dot{z} + \dot{y}\dot{s}\dot{z})^2$$
 (17)

$$I_y = I_{1y} - w(xs2^2 + zs4^2) + w(xs2 + xs4)^2 + w(zs1 + zs4)^2$$
 (18)

$$I_z = I_{1z} - w(x s2^2 + ys2^2) + w(xs2 + xs4)^2 + w(ys2 + ys4)^2$$
 (19)

$$I_{XZ} = I_{XZ} - W (XS2) (ZS4) + W (XS2 + ZS4) (ZS4 + ZS4)$$
 (20)

For outboard surfaces:

$$I_x = I_{OX} + W (YS3 + b_2 \cos \theta + YS4)^2 + W (ZS1 + b_2 \sin \theta + ZS5)^2$$
 (21)

$$I_v = I_{ov} = W (XS5 + XS3)^2 + W(ZS1 + b_2 \sin\theta + ZS5)^2$$
 (22)

$$I_z = I_{oz} + W (YS3 + b_2 \cos \theta + YS4)^2 + W (XS5 + XS3)^2$$
 (23)

$$I_{xz} = I_{OXZ} - W (ZS3) (ZS5) + W (XS3 + XS4) (ZS5 + ZS1)$$
 (24)

B. FUSELAGE

The fuselage data needed for inertia calculations is:

Fuselage weight is divided into four areas:

- 1. Structure
- 2. Distributed contents
- 3. Volumes of mass
- 4. Point masses
- 1. Structure. Fuselage structural weight includes wing carry-through structure (if it was added to the fuselage group) and air induction system weight (if you have buried engine installations). This weight is assumed to be distributed between a conical nose shell, open-ended right-cylindrical shell, and a conical tail shell. For buried engine installations, the conical tail shell is neglected. Fuselage structure is distributed to each geometric shape in proportion to the surface area. (weight area constant). Air induction

system weight should be added to the open ended right-circular shell.

Moments of inertia of fuselage sturcture about the remote axes (see
Appendix, Section 3) are given by:

$$I_{x} = \frac{R^{2}}{2} (W_{n} + 2 W_{c} + W_{t}) + W_{s} (Z_{b})^{2}$$
(25)

$$i_{y} = \frac{R^{2}}{4} (W_{n} + 2 W_{c} + W_{t}) + 1_{n}^{2} (\frac{W_{n}}{2} + W_{c} + W_{t}) + 1_{c}^{2} (\frac{W_{c}}{3} + W_{t}) + \frac{1}{2} \frac{W_{t}}{6} + \frac{1}{2} \frac{1}{n} (W_{c} + 2W_{t}) + \frac{2}{3} \frac{1}{1} \frac{1}{n} \frac{W_{t}}{4} + \frac{2}{3} \frac{1}{1} \frac{1}{n} \frac{W_{t}}{4} + \frac{W_{s}}{3} (Z_{b})^{2}$$
(26)

$$I_z = I_v - W_s (Z_b)^2$$
 (27)

$$I_{xz} = W_n (3/4 \ 1_n \ Z_b) + W_c Z_b (1n + \frac{1c}{2}) + W_t Z_b (1_n + 1_c + \frac{1t}{4})$$
 (28)

2) <u>Distributed Contents</u>. This consists of four main items. electrical system, instruments and navigation, hydraulics, and surface controls. They are assumed to be randomly spread throughout the fuselage from the cockpit to the leading edge of the horizontal tail in the shape of an open ended right-cylindrical shell. Moments of inertia of distributed contents about the remote axes (see Appendix, Section 4) are given by:

$$I_x = W_{dc}R^2 + W_{dc}(Z_b)^2$$
 (29)

$$I_y = \frac{W_{dc}}{2} (R^2 + 1/6 (XS4-CREW_{cg}))^2) +$$

$$W_{dc} \left(\frac{xs4 - CREW}{cg} + \frac{CREW}{cg} \right)^2 + W_{dc} z_b^2$$
(30)

$$I_z = I_y - W_{dc} (Z_b)^T$$
 (31)

$$1_{xz} = \frac{W_{dc}}{\frac{dc}{2}} (XS4 + CREW_{cg}) (Z_b)$$
 (32)

Here W_{dc} is defined as the weight of surface controls allocated to the fuselage + weight of electrical system allocated to the fuselage + weight of hydraulic system allocated to the fuselage + 30% of weight of instruments and navigation allocated to the fuselage.

3) Volumes of Mass consist of items such as the fuel system in the fuselage, the avionics bay, and furnishings. It is left to the user to decide whether to use these as volumes or point masses because of the variability of the items. Either a cylindrical shell or a solid rectangular shape can be used. Moments of inertia of these volumes about the remote axes (see Appendix, Section 5) are given by:

Cylindrical shell - (33)
$$I_{x} = W_{vo} R^{2} + W_{vo} Z^{2}$$

$$I_y = \frac{W_{vo}}{2} (R_v^2 + \frac{1}{6}^2 + W_{vo} (X^2 + Z^2))$$
 (34)

$$I_{z} = \frac{W_{vo}}{2} \left(R_{v}^{2} + \frac{1}{6}^{v_{2}} \right) + W_{vo} X^{2}$$
 (35)

$$I_{XZ} = W_{VO}^{XZ} \tag{36}$$

Rectangular solid -

$$I_x = \frac{W_{vd}}{12} (2R_v^2 + 2R_v^2) + W_{vo}Z^2$$
 (37)

$$I_{y} = \frac{W_{vo}}{12} (1_{v}^{2} + 2R_{v}^{2}) + W_{vo} (x^{2} + z^{2})$$
 (38)

$$I_z = \frac{W_{vo}}{12} (1_v^2 + 2R_v^2) + W_{vo}x^2$$
 (39)

$$I_{XZ} = W_{VO}XZ \tag{40}$$

4. <u>Point Masses</u>. Each point mass is generally considered separately for calculating inertias. Aggregate small items, such as troop provisions in cargo aircraft are handled differently. For roll (I_x) inertia the point mass total weight for aggregate items is distributed between a solid cone and a solid right circular cylinder. All aggregate point masses located in the nose or tail cone of the fuselage are put in the solid cone and all point masses in the center section are put in the solid right circular cylinder. For I_y and I_z they are lumped at some average location. The moment of inertia of point masses about the remote axes (see Appendix, Section 6) are given by:

$$I_{x} = \Sigma W_{p} (Y^{2} + Z^{2})$$

or

$$I_x = \frac{\text{Wpc}}{2} R^2 + \frac{3}{10} \text{ Wpnc } R^2 + (\text{Wpc} + \text{Wpnc}) (Z_b)^2$$
 (41)

$$I_y = \Sigma W_p (x^2 + z^2)$$
 (42)

$$I_{x} = \Sigma Wp (X^{2} + Y^{2})$$

$$(43)$$

$$I_{xz} = \sum_{p} XZ \tag{44}$$

Items usually considered as point masses:

Main and nose landing gear

Auxiliary power unit

Air Conditioning

Auxiliary gear

Gun

Crew

Armament

Surface controls assigned to cockpit

Radar

Photographic

70% of instruments and navigation weight (locate at cockpit)

Other equipment

Liquid nitrogen

Miscellaneous items

C. Propulsion

The propulsion data needed for inertia calculations is: W_e , R_e , e, I_e , XP, YP, ZP, I_o of engines.* The total group weight is divided by the number of engines; this is the weight of each engine and accessories. If the I_o 's of the engines are not known, they can be approximated by using a solid cylinder (see Appendix, section 9). The moments of inertia of each engine about the remote axes are given by:

I approximated:

$$I_x = \frac{W_e R_e^2}{2} + W_e (YP^2 + ZP^2)$$
 (45)

$$I_{y} = \frac{V}{12} (3R_{e}^{2} + I_{e}^{2}) + W_{e} (XP^{2} + ZP^{2})$$
 (46)

$$I_z = \frac{W_e}{12} (3R_e^2 + 1_e^2) + W_e (XP^2 + YP^2)$$
 (47)

$$I_{XZ} = W_{e} (XP) (ZP)$$
 (48)

I input:

$$I_x = I_{ox} + W_e (YP^2 + ZP^2)$$
 (49)

$$I_y = I_{oy} + W_e (XP^2 + ZP^2)$$
 (50)

$$I_z = I_{oz} + W_e (XP^2 + YP^2)$$
 (51)

$$I_{xz} = I_{oxz} + W_{e} (XP) (ZP)$$
 (52)

 $[*]R_e$ and l_e are not needed if inertias are given.

D. Internal Fuel

1. Wing fuel tanks

Internal wing fuel is defined in the same manner as surfaces because of the wing fuel tank shape being similar to a surface. We assume the wing tank is full of fuel and has a constant density. The I equations for surfaces (see Appendix, Section 2) can now be used as long as we substitute ρ (density of fuel) for $\frac{W}{V}$.

$$I_{4X} = 2b^3 \rho \left[-(t_r - t_t) \left(\frac{c}{4} + \frac{b}{5} \left(\tan \Lambda_T - \tan \Lambda_L \right) \right) + t_r \left(\frac{c}{3} + \frac{b}{4} \left(\tan \Lambda_T - \tan \Lambda_L \right) \right) \right] (53)$$

$$I_{4y} = 2b\rho \left\{ \frac{t}{r} \frac{(c^3 + bctan \Lambda_T)}{3} + \frac{btan \Lambda_T}{3} + \frac{b^3}{12} (tan^3 \Lambda_T - tan^3 \Lambda_L) \right\}$$

$$\left[(t_r - t_t) \frac{(c^3 + bctan \Lambda_T)}{6} + \frac{btan \Lambda_T}{3} + \frac{b^3}{15} (tan^3 \Lambda_T - tan^3 \Lambda_L) \right] \right\}$$
(54)

$$I_{4z} = I_{4x} + I_{4y} \tag{55}$$

Again realizing wing fuel tanks may be at some dihedral angle:

TRUE
$$I_{4y} = (I_{4y} \cos \theta + I_{4z} \sin \theta)$$
 (56)

TRUE
$$I_{4z} = (I_{4y} \sin \Theta + I_{4z} \cos \Theta)$$
 (57)

 I_{4x} is not affected by dihedral. If there is dihedral, the product of inertia of the fuel is given by:

of the fuel is given by:
$$I_{4xz} = 2\rho \sin \Theta \left[t_{T} \left(\frac{c^{2}b^{2}}{12} + \frac{cb}{12} \right)^{3} \tan \Lambda_{T} + \frac{b^{4}}{40} \left(\tan^{2} \Lambda_{T} - \tan^{2} \Lambda_{L} \right) \right] + t_{T} \left[\frac{c^{2}b^{2}}{6} + \frac{cb^{3}}{4} \tan \Lambda_{T} + \frac{b^{4}}{10} \left(\tan^{2} \Lambda_{T} - \tan^{2} \Lambda_{L} \right) \right] \right\}$$
(58)

These equations calculate the total I₄ for total wing fuel (right and left wing fuel tanks).

TABLE 4
WING INTERNAL FUEL TANK SYMBOLS

General Symbol	Defined Symbol
$^{\Lambda}_{ extbf{L}}$	Λ г 3
${^{\boldsymbol{\Lambda}}}_{\mathbf{T}}$	$^{\Lambda}_{ exttt{T3}}$
Ъ	b ₄
c	c ₃
^t r	t f
t _t	t _f o1bc
ρ	$JP4 = .02814 \frac{1b}{in}3$
X X	XF1
¥ Y	y ř l
= Z	ZF2

Again, as in the case for surfaces, the centroid of the fuel tank must be calculated. The centroid is assumed to be located at the center of volume of the tank. (See Appendix, Section 7.)

of volume of the tank. (See Appendix, Section 7.)

$$XF1 = \frac{b}{v} \left\{ \left[\left(t_{r} \left(\frac{c^{2}}{2} + \frac{bctan\Lambda_{T}}{2} + \frac{b^{2}}{6} \left(tan^{2} \Lambda_{T} - tan^{2} \Lambda_{L} \right) \right) \right] \right. (59)$$

$$- \left[\left(t_{r} - t_{t} \right) \left(\frac{c^{2}}{4} + \frac{cbtan\Lambda_{T}}{3} + \frac{b^{2}}{8} \left(tan^{2} \Lambda_{T} - tan^{2} \Lambda_{L} \right) \right) \right] \right\}$$

$$YF1 = \frac{b^{2}}{v} \left[t_{r} \left(\frac{c}{2} + \frac{b}{3} \left(tan\Lambda_{T} - tan\Lambda_{L} \right) \right) \right] - \left[\left(t_{r} - t_{t} \right) \left(\frac{c}{3} + \frac{b}{4} \right) \right]$$

$$\left(tan\Lambda_{T} - tan\Lambda_{L} \right) \right]$$
(60)

The vertical fuel tank centroid is zero unless the wing has anhedral or dihedral, in which case:

ZF2 = YFl sin 0

The fuel tank I_4 can be translated to obtain I_6 and then I by:

$$I_x - I_{4x} - W_{fw} Y\dot{F}1^2 - W_{fw} (ZF2)^2 + W_{fw} (Y\dot{F}1 + YF2)^2 + W_{fw} (ZF^2 + ZF)^2$$
 (61)

$$Iy = I_{4y} - W_{fw} XF1^2 - W_{fw} ZF2^2 + W_{fw} (XF1 + XF2)^2 + W_{fw} (ZF2 + ZF)^2 (62)$$

$$I_z = I_{4z} - W_{fw} (XF1^2 + YF1^2) + W_{fw} (XF1 + XF2)^2 + W_{fw} (YF1 + YF2)^2$$
 (63)

$$I_{xz} = I_{4xz} - W_{fw} (XF1)(ZF2) + W_{fw} (XF1 + XF2)(ZF2 + ZF)$$
 (64)

If there is more than one internal wing fuel tank, this total procedure can be used for each subsequent tank in the same manner.

2. Fuselage Fuel Tanks

Fuselage internal fuel is assumed to be in the shape of a solid right cylinder. These inertia calculations are to be used in aircraft flying qualities studies; only short period rolling motions will be examined, and the fuel will not attain any appreciable rotational motion during these maneuvers. The rolling inertia of the fuel about its own axis is therefore assumed to be zero. The moments of inertia of fuselage internal fuel about the remote axes (see Appendix, Section 8) is given by:

$$I_{OX} = 0 \tag{65}$$

$$I_{\text{oy}} = \frac{W_{\text{ff}}(W_{\text{ff}}}{12} + I_{\text{f}}^{2}) + W_{\text{ff}} (X^{2} + Z^{2})$$
 (66)

$$I_{oz} = \frac{W_{ff}(W_{ff} + 1_f^2) + W_{ff}X^2}{\Pi \rho 1_f}$$
 (67)

$$I_{oxz} = W_{ff} XZ \tag{68}$$

E. Payload

1. Transport Payload

Payload inertia is estimated by using a solid rectangular mass or series of masses as were the volumes of mass in the fuselage. Moments of inertia for payload about the remote axes (see Appendix 5, Section 9) are given by:

$$I_{x} = \frac{W}{12} (d_{p}^{2} + d_{p}^{2}) + WZ^{2}$$
 (69)

$$I_{y} = \frac{W}{12} (I_{p}^{2} + d_{p}^{2}) + W (X^{2} + Z^{2})$$
 (70)

$$I_z = \frac{W}{12} (I_p^2 + d_p^2) + WX^2$$
 (71)

$$I_{xz} = WXZ \tag{72}$$

2. Internal Weapons

It is assumed that the inertia and locations of these items are given.

F. Additional Items

1. External Stores and Tanks

Wing and fuselage store and tank pylons are to be used as point masses to calculate I_x , I_y , and I_z . External wing and fuselage tanks and stores can be approximated by shells and solid right cylinders (s.e Appendix, Section 9) depending on whether the tanks are full or empty.

TANKS:

$$I_z = \frac{W_{st}}{2} (\underline{SR}^2 + \underline{SL}^2) + W_{st} (Y^2 + X^2)$$
 (73)

$$I_y = \frac{W_{st}}{2} (SR^2 + \frac{SL^2}{6}) + W_{st} (X^2 + Z^2)$$
 (74)

$$I_x = W_{st} SR^2 + W_{st} (Y^2 + Z^2)$$
 (75)

$$I_{xz} = W_{st}XZ \tag{76}$$

STORES:

$$I_{x} = \frac{W_{st}}{2} SR^{2} + W_{st} (Y^{2} + z^{2})$$
 (77)

$$I_y = \frac{W_{st}}{12} (3 SR^2 + SL^2) + W_{st} (X^2 + Z^2)$$
 (78)

$$I_z = \frac{W}{\frac{8}{12}} (3 SR^2 + SL^2) + W_{8t} (X^2 + Y^2)$$
 (79)

$$I_{xz} = W_{st} XZ \tag{80}$$

G. Total Aircraft Inertias

The total inertia about the remote axes from all groups are now summed to achieved a complete inertia for the total aircraft. For this to be translated back to the center of gravity of the total vehicle, the center of gravity location must first be calculated. By definition:

$$\frac{\mathbf{X}}{\mathbf{X}} = \mathbf{\tilde{\Sigma}} \frac{\mathbf{W} \mathbf{X}}{\mathbf{X}} - \mathbf{\tilde{\Sigma}} \frac{\mathbf{W} \mathbf{Z}}{\mathbf{Y}} = 0$$
 (81)

where X and Z are distances to the item or group centroid. All item and group weights and distances to the remote axes are already known, except for the fuselage structure longitudinal distances. These are given by:

WX nose cone =
$$W_n$$
 (2/3 l_n) (82)

WX center =
$$W_c (1_n + 1/2 1_c)$$
 (83)

WX tail cone =
$$W_t (l_n + l_c + 1/3 l_t)$$
 (84)

W should equal the total aircraft weight. \overline{Y} is zero because of the already assumed symmetry of the aircraft. The translation of the total inertias to the aircraft center of gravity is then:

$$I_{cgx} = I_x - \frac{2}{WZ}$$
 (85)

$$I_{cgy} = I_y - W(\overline{Z}^2 + \overline{X}^2)$$
 (86)

$$I_{cgz} = I_z - W X^2$$
 (87)

$$I_{\text{cgxz}} = I_{\text{xz}} - \overline{\text{wxz}}$$
 (88)

Results from the use of this method on various types of aircraft is given in Table 5. Data on these aircraft were obtained from References 3 - 6.

(Moments of Inertia X10 - $^{-6}$) (1b - in²)

Table 5. Summary Comparison

Configuration	Ro11	• ·	Pitc	h	Yaw	
F-15A	Actual	Calc.	Actual	Calc.	Actual	Calc.
Operating Weight Empty	97.8	129.0	747.2	762.2	822.3	835.6
Air Superiority Takeoff Weight	166.5	190.8	824.0	829.2	946.0	951.8
<u>C-5A</u>						
Operating Weight Empty	57909	54246	101486	98853	146944	140694
Basic Flight Design Max Fuel	170867	158941	124744	116564	279748	266755
<u>A-10</u>						
Weight Empty	168	203	413	356	580	543
Ferry Mission Gross Weight	293	279	604	608	817	891
<u>B-52G</u>						
Weight Empty	26011	23270	22551	19380	48562	42216
Design Gross Weight	69163	64142	39520	37350	108683	92696
Average Error (%)	·	11.4		5.7		6.8

Average percent error of actual versus calculated values is 8.6%

(Moments of Inertia X10⁻⁶) (1b - in²)

III. Sample Problem: C-5A

MAN MITTERS

the second the second s

Moments of inertia are first calculated for operating weight empty and then for basic flight design weight with maximum fuel. All units are pounds and inches. Basic geometry and weight data are given in Figures 1 and 2 and Tables 6 and 7. This data was taken from Reference 3.

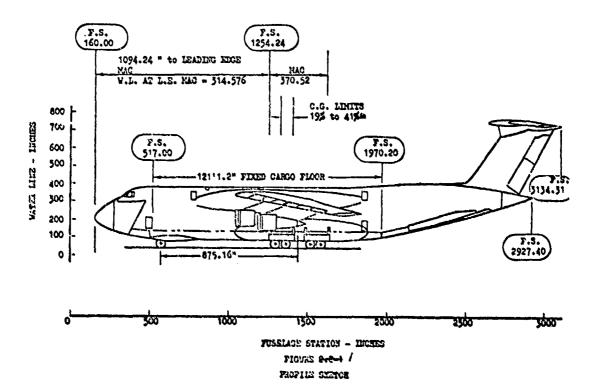


Figure 2. C-5A Three-View

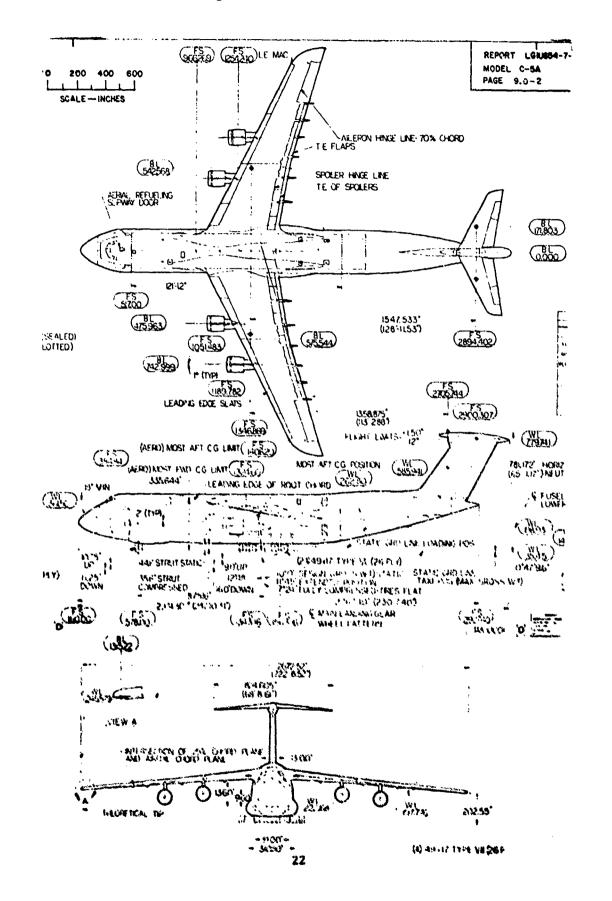


Table 6. C-5A Weight Statement

							
7	WING CROUP		,		· ·		
-	BASIC STRUCTURE - CENTE	~~~~~~~		ļ			82044.8
i	= TATER	TECTATE"	PANET	 		9661.2 1:036.4	
2	- OUTER			}		13150.0	
ē	SE CONDARY STRUCTURE					3729.8	
7	ALERONS TINCLUUTING 916	L B BAL	AVCE WET	6417		2327.0	
Ē	FLAPS - TRAILING EDGE			 		10736.8	4
3	SLAIS - LEADING EDGE			 		VA:5.U	
Ť	SPOILERS					2474.8	
Н	3. 02223			 			'
爿							
3	TAIL GROUP		 	 			12335.
-	STABILIZER - BASIC STRU	TURE		·		4711.9	
Ė	- SECONDARY		<u>L</u>	 		979.9	, •
Ξ	- ELEVATOR T			PALANCE	NE TORY T	15:1.2	
7	FIN - JUST C STRUCTURE !		 			757765	
9	- SECOND ARY STRUCTU	RE	 -	 		348.7	
Ē	~ RUDDER		 	 		678.7	
τ			 	1			7
i			 	 			
7	BODY GROUP LINCLUDING M	AKOF ACTO	RING VAR	TATION	F -27 21	<u> </u>	116047.5
7	FUSELAGE - BASIC STRUCT	UR E	T	1		61394.8	
4	GEAR POUS TINCLUCING ME		ובאסטט סי	·		35 E T • 2	Y
=	CARGO FUDOR CINCUUDING			•	LEST	17074.11	
E	RAILS AND RULLERS THESE		•	ļ		2536.5	
7	FUSELAGE - SECONDARY ST		(1		E308.2	<u></u>
	FORWARD LOAD ING DOCK'S			<u> </u>			! 7
75			UKI	i			1./
7 :				TEET		5372 o 3	
7 E	FORWARD RAMP CINCUUDING	RAMP E	CLEA 2 I.CM.	TCET		4375.5	Y
?	FORWARD RAMP LINCUUDING AFY CADING COORS ISIDE	RAMP E)	RI	İ		7238.1	7
?! !(FORWARD RAMP CINCUUDING	RAMP E)	RI	İ		4375.5	7
? : !(FORWARD RAMP LINCUUDING AFY CADING COORS ISIDE	RAMP E)	RI	İ		7238.1	7
7	FORWARD RAMP LINCUUDING AFY CADING COORS ISIDE	RAMP E)	RI	İ		7238.1	7
	FORWARD RAMP (INCLUDING AFT CADING DOORS ISIDE AFT RAMP (INCLUDING PRE	RAMP E)	RI	İ		7238.1	7
	FORWARD RAMP (INCLUDING AFT CCADING DOORS TSIDE AFT RAMP (INCLUDING PRE	RAMP E)	CTEVSTON RI DR + TOE			7238.1	7
	FORWARD RAMP (INCLUDING AFT CADING DOORS TSIDE AFT RAMP (INCLUDING PRE	TAMPE) TENTE SSURE DO	CTENSTON RI OR + TOE		ECNI RCLS	7375.6 7736.1 6483.1	7
	FORWARD RAMP (INCLUDING AFT CADING DOORS TSIDE AFT RAMP (INCLUDING PRE	TAMPE) TENTE SSURE DO	CTENSTON RI OR + TOE		CONTROLS	7375.6 7736.1 6483.1	7
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PREALISHYING SEAR GROUP	TAMP E) TENTE SSURE DO	RI BUR + TOE BUR + TOE ROLLING	; ; ; ; ; ;	<u> </u>	7375.6 7736.1 6483.1	38087.9
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PREALISTYING SEAR GROUP	TAMP E) TENTE SSURE DO	HOLEING HOLE IN THE PROPERTY OF A PROPERTY O	ST RUCT	6412.2	775.6 7736.1 6483.1	38087.9
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PRE	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A PROPERTY O	; ; ; ; ; ;	6412.2	775.6 7736.1 6483.1	38087.9
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PREALISTYING SEAR GROUP	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A PROPERTY O	ST RUCT	6412.2	775.6 7736.1 6483.1	38087.9
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PREALISHYING SEAR GROUP	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A PROPERTY O	ST RUCT	6412.2	775.6 7736.1 6483.1	38087.9
	FORWARD RAMP (INCLUDING AFT LCADING DOORS ISIDE AFT RAMP (INCLUDING PREALISHYING SEAR GROUP)	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A PROPERTY O	ST RUCT	6412.2	7375.6 7236.1 6483.1 7CTALS 33680.9	38087.9
	FORWARD RAMP (INCLUDING AFT ECADING DOORS ISIDE AFT RAMP (INCLUDING PREALISTING SEAR GROUP) AUTHUR SEAR GROUP SURFACE CONTROLS GROUP COUNTIL CONTROLS	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7736.1 6483.1 707405 35680.9 7407.0	38087.9
	FORWARD RAMP (INCLUDING AFT ECADING DOORS ISIDE AFT RAMP (INCLUDING PREALIBITION OF ALIBRITA CONTROLS GROUP COUPT CONTROLS AUTOMATIC PILUT	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	7975.6 7236.1 6483.1 7074LS 35680.9 7407.0	38087.9
	FORWARD RAMP INCLUDING AFY ECADING COORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP SURFACE CONTROLS GROUP COUPTI CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7736.1 6483.1 707405 35680.9 7407.0	38087.9 7 F34
	FORWARD RAMP (INCLUDING AFT ECADING DOORS ISIDE AFT RAMP (INCLUDING PREALITATION OF THE COUPT COUPT COUPT CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS	TAMP E) TENTE SSURE DO LUCATION	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	7975.6 7236.1 6483.1 7074LS 35680.9 7407.0	38087.9 7 F34
	FORWARD RAMP (INCLUDING AFT ECADING DOORS ISIDE AFT RAMP (INCLUDING PREALITHING SEAR GROUP) AUTHORS CONTROLS GROUP COUPTI CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS	HAMPE) CENTESSURE DO LUCATION MATN NOSE	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	7975.6 7236.1 6483.1 7074LS 35680.9 7407.0	38087.9 7 F341
	FORWARD RAMP INCLUDING AFY ECADING DOORS IS IDE AFY RAMP LINCLUDING PREAFIGROUP ALIGHYING SEAR GROUP SURFACE CONTROLS GROUP COURTT CONTROLS AUTOMATIC PICT SYSTEM CONTROLS	HAMPE) CENTESSURE DO LUCATION MATRINOSE	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7736.1 6483.1 707465 73680.9 7407.0	38087.9 7 F341
	FORWARD RAMP INCLUDING AFY ECADING COORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP COUPLY CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS THEOARD - POO STRUCTURE	HAMPE) CENTESSURE DO LUCATION MATRINOSE	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7236.1 6483.1 707405 35680.9 7407.0 151.5 6866.1	38087.9 7 F341
	FORWARD RAMP INCLUDING AFY ECADING COORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP COUPLY CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS 2 13 INE SECITOR OR NACELUE 1 180 ARD - PCD STRUCTURE - PYLON	HAMPE) CENTESSURE DO LUCATION MAIN NOSE GROUP	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7236.1 6483.1 7074LS 35680.9 7477.0 151.5 6866.1	7 F 3 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	FORWARD RAMP INCLUDING AFY ECADING COORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP COUPLY CONTROLS AUTOMATIC PILUT SYSTEM CONTROLS 2 13 INE SECITOR OR NACELUE 1 180 ARD - PCD STRUCTURE - PYLON OUTEGARD - PCD STRUCTURE	HAMPE) CENTESSURE DO LUCATION MAIN NOSE GROUP	HOLEING HOLE IN THE PROPERTY OF A TOPE TO THE PROPERTY OF THE	ST RUCT	6412.2	775.6 7236.1 6483.1 707405 35680.9 7407.0 151.5 6866.1	7 F 5 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	FORWARD RAMP INCLUDING AFY ECADING DOORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP COUPTI CONTROLS AUGUSTIC PILUT SYSTEM CONTROLS THEORY - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON	HAMPE) CENTESSURE DO LUCATION MAIN NOSE GROUP	INCE SIGNAL HOLEING HOL	ST RUCT	6412.2	7375.6 7236.1 6483.1 707405 35680.9 7407.0 116.0 151.5 6866.1	7 F 5 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
	FORWARD RAMP INCLUDING AFY ECADING DOORS ISIDE AFY RAMP LINCLUDING PRE ALIGHYING SEAR GROUP COUPTI CONTROLS AUGUSTIC PILUT SYSTEM CONTROLS THEORY - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON OUTECARD - POD STRUCTURE - PYLON	HAMPE) CENTESSURE DO LUCATION MAIN NOSE GROUP	INCE SIGNAL HOLEING HOL	ST RUCT	6412.2	775.6 7236.1 6483.1 707405 35680.9 7407.0 151.5 6866.1	7 F 3 4 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1

Table 6-continued

-11		T	~ 			······································	
2	900 אט אט אט אט פאס			1			38281.1
-3	ENGINE INSTALLATION					2917772	
	AFTERBURKERS (TF FURNIS	HED SEPA	RATELYT				
-ř.	ACCESSORY SEAR BOXES AN	C-DRIVE'S	reser			• 6	
E	SUPERCHARGERS (FOR TURE	123 4V T				•0	
7	AIR INCUCTION SYSTEM					•0	
9	EXHAUST SYSTEM					218.4	/
- 3	COCLING SYSTEM				-,	3.67	
TO	CUBRICATION SYSTEM					10.4	
П	TANKS						
13	COOLING SYSTEM						
13	PUCYS. PLUKEING, EYC.						
Ti	FUEL SYSTEM					7457.8	
1:	TANKS - HING				\$ 617.2		
Te	- 330Y					·	
17	PEUKSING, ETC.			 	1817.6	2	
1 8	HATER INJECTION SYSTEM					.0	
10	ENGINE CONTROLS					178.2	/
20	STARTING SYSTEM	-			· 	137.5	
21	THRUST REVERSERS			·		3949.4	1
7.5				l			\ <u>'</u>
2.3	AUXILIARY POWER PLANY GRO	UP					3.25.E
24							
7.5	INSTRUMENTS AND NAVIGATIO	NAL EQUI	PHENT GR	CUP			V936.8
2.5	The second secon						
7.7	HYDRAULIC GROUP		··				7 3978.5
23							
23	ELECTRICAL GROUP					· · · · · · · · · · · · · · · · · · ·	¥ 5450.8
30		· 					
3.1	ELECTRONICS GROUP						388.3 * 5
3 6	EGUIPHENT					2571.5	-
33	INSTALLATION					1315.1	
3.4							*******
3.2	ARMAHENT GROUP				~~~		
35							/
77	FURNISHINGS AND EQUIFMENT	CRUUP				······································	75835.5
TE	ACCOMMODATIONS FOR PERS	Q A N.EE				21 50 - 1	*
े अ	MISCELLANECUS EGUIFHENT					965.1	
3(0)	FURNISHINGS					3535.9	
वा	ENERCENCY EQUIPMENT		·			1 E 3 . E	
4 2							
13			**************				
4.4							
14.5							
₹ €	AIR CONDITIONING AND ARTI	- 10176 3	יין די				75640.0
7	AIR CONDITIONING					3411.1	
4.9	ANTI-YCING					25.9	
भिष्							
รบ	AUXICIARY GEAR GROUP						14:4
12.1	HANDEING SEAR					36.6	
183	ARRESTING GEAR					·U	
15.3	CATAPULTING GEAR					1.	
[]	***						
1:5	HANUFACTURING VARIATION		IN BCOV	GRECEPT			0/402- 41
[5]	TOTAL FROM PRECESSING PAG	F					265297.1
1:1	WEIGHT EKPTY						325263.6

Table 6-continued

1			BASIC WEIGHT	OPERAT.	O.W. +	FLT DES
2 LOAD CONDITION			METOUT	MSTOUT	HIC -	PIAL CAN
4 CREW (NO. 6) (INCLUDING	BAGGAGET	 	0	1,290	1,290	1,290
E COLUMN TO THE STATE OF THE ST	Divor			1=2	1	1-1-7
.6						
7 FUEL	IYPE	GAL				
8 UNUSABLE	JP-4	87	562	562	562	562
d INTERNAL	JP=4	0	0	0	0	
IO INTERNAL	JP=4	28,322				184,096
11 INTERNAL	JP =4			l		
12 INTERNAL	JP=4	<u> </u>		i		
13		<u> </u>	i		<u> </u>	
1 4		<u> </u>			<u> </u>	
15 OIL	<u> </u>	<u> </u>			<u> </u>	
16 TRAPPED	<u> </u>		58	58	58	58
17 ENGINE			0	206	206	206
18		 			ļ	
19	<u> </u>			ļ	ļ	ļ
<u> 20 RAGGAGE - CREW (INCLUDED</u>	IN CREW	MEIGHTL		Ì	<u> </u>	
21 TIEDOWN DEVICES	<u> </u>		1.750	1.750	1,750	1,750
22		ļ	ļ		ļ	ļ
23	 	ļ		7-5		1.22. 22
24 PAYLOAD			(7,581)	(0)	(7,581)	(214,45
25 DELIVERABLE CARGO		ļ				ļ
26 AUXILIARY CREW		ļ	ļ	ļ	ļ	
27 BAGGAGE		 				
28 PASSENGERS/TROOPS	<u></u>	 				
29 PALLETS (300 LB EA	CHI				ļ ———	6,600
30 PALLET LETS (54 LB 31 PALLET LOAD 32 VEHICLES	-EACH)			ļ		1,188
31 PALLET LOAD 32 VEHICLES		 			ļ	193,405
33 CHAINS (IN EXCESS OF 1	750 LB)	<u> </u>		ļ	ļ	
	GO LOT					206
34 WRM KIT 35 REMOVABLE TROOP PROVI	SLOUS TODY		7,581		7,581	680 7,58
36 AFT TOE RAMPS	21042 (17.11		(1)261		7,551	1-11-3
NO AFT TOE KARES						
37 38		 			 	
va Na						 -
39 40	 					
Ä J					 	
						 -
NS EQUIPMENT	·					
PYRGIECHITES					·	 -
AS PHOTOGRAPHIC						
NO LIFE RAFTS - CREW (YM	THE EQUIPMENT	\ <u></u>	500	200	ટળ	200
NY OXYGEN - CARY (25 LITERS	X	1	63	63	6)	200 63 17
			17	19	17	1
WATER - CREA			43	43	43	4)
50 ¹	1	·		<u>-</u> -	1	
HU FOOD - CREM 49 WATER - CREM 50 51 51	1					1
52	 				 	
53 54		· · · · · · · · · · · · · · · · · · ·			<u> </u>	
	1	<u> </u>				
55 USEFUL KOAD			10,274	4,189	11,770	102,757
	1	ž .	10.2/9	74107		
SE WEIGHT EMPTY			329,265	325,265	5:5,263	121,263

Table 6-continued

S LOVO COUDITION	- 	T	FLT DES	MAX DES	HAX DES	YERRY
3			MAX FUEL	MAX CAR	KAX FUEL	EISSICE
" CREW (NO. 6) (INCLUDING	AGGAGE)	}	1,290	1,290	1,200	1 200
5	7	i	1 - 11 - 22	1,220_		1,299
6		İ				
7 FUEL	TYPE	GAL.				
6 UNUSABLE	JP=4	ε7	562	562	562	562
9 INTERNAL	J4-4	49,000	318,500		318,500	318,500
O. INTERNAL	JP-4	27,707		180,096		
1 INTERNAL	JP-4					
2 INTERNAL.	JP-4	l				
3	<u> </u>	<u> </u>				
4	<u> </u>	<u> </u>				
5 01L	<u> </u>	! !				
6 TRAPPED	.		58	58	58	58
7 ENGINE		<u> </u>	206	206	206	206
8	 	<u> </u>	<u></u>			
9	<u> </u>	!	ļ			
O BAGGAGE - CREW (INCLUDED	IN CKEW	WE I GHIT				
1 TIEDOWN DEVICES			1,750	1,750	1,750	1,750
3		ļ	ļ			
3	- 		700 0107	(050 150)	101 0101	75 55
4 PAYLOAD		 	[[00,040]	(259,452)	121,048)	(7,581
DELIVERABLE CARGO			·			
6 AUXILIARY CREW		 	·			
7 BAGGAGE	J	ļ	 		<u></u>	
8 PASSENGERS/TROOPS		 	l			
PALLETS (300 LB EA	CH)	'	2.400_	7,800	3.600 648	
O PALLET NETS (54 LB	-EACH)	'	432	1,404		l
1 PALLET LOAD		 -	68,955	241,987	108,539	<u> </u>
VEHICLES	1 (1)	 	<u> </u>		}	}
3 CHAINS (IN EXCESS OF	1750 LB)	 				ļ
WRM KIT	CIONE TOO		7,581	680 7,581	7,581	7,581
S REMOVABLE TROOP PROVI	SIONS (DI	11	1-10 Sur		7, 301	7, 701
AFT TOE RAMPS		 			}	
57		{		<u> </u>	l 	
58	ᆛ		·	<u> </u>		
39		 	·			 -
10		 	 			
12		 	-	 		
S EQUIPMENT		 		{·· ·-	—	· , · · · · · · · · · · · · · · · · · ·
14 PYROTECHNICS		 	- · -	-		-
15 PHOTOGRAPHIC	 	 				
	-		200	200	200	200
16 LIFE RAFTS - CREW (DEC.	L-EQUIPME	·	200	200 63	200	200
7, OXYGEN - CREW (25 LITERS	4	 	17	17	17	17
19. WATER - CREW		 	43	43	43	1.4 1.7
50; WATER - CREW			1			
51		·	-	 	 	
~ ^!. <u>~</u>		 	-			
52	_{	 	 			
55 <u></u>	_					The State of
USEFUL LOAD		-	402,737 325,263 722,6337	443,737	343.737	330,270
		حد سحد سحد الم	-1.1257.171.1	1-32-11-55	1327777	525,26 <u>5</u>
SO WEIGHT CMPTY			1 202 002 .	325,265\ 700,000	324, 264	1 2.34 AM. A

Table 7. C-5A Geometric Data

ட்	LENGTA - OVERALL (FIT Y	i).e∈	HE1641	- CVERA	CUTIFFT T		
L3	LOADARCE	LOADABLE	LOACABLE				
3		AFT	CARGC	CARGO		NACELLES	7510E
	1 4111		FLCCR	CCKPT	FUSE.	INBC	CUIBD
	LENSTH - MAX (F) 3.	13.4	1,519	144.8	230.6	5.6.0	28.7
E	DEPTH - HAX (F ()			3.5	25.9	2.5	8.2
	1	0.81	79.3		23.9	8.2	9.5
E	"- " - " TO " TO " TO " TO TO	† 	·		16645.7	969	189.2
3	FLAT SURF (SO FY) 186.	254.6	2300.3	2741.5			
π	FUSE VOLUME (CU FT)	† 	PRESSURT	ZEO	EEE31.7		
П			TOTAL		96610.1		
Tè							
Li		<u> </u>	<u> </u>		DING	H. TAIL	V. TAIL
14	GROSS AREA (SG. FT)		ļ		62110.10	36 2 62	
E	EXPOSED PLANFORM AREA ISS	FYJ	 		5377.5	872.9	252.7
17	SPAN (FT)	 			22201	EE-7	:405
	1 -	1777	 		10359.2	1943-6	116511
	STRUCTURAL BOX ATOTH AT &	1	TION TIN		240.4	111-4	196.5
	SWEEPBACK AT ZE . CHCRD			í i		1	31.3
71	1			TCTIP	25.00	- 24 - 5	34.3
21	1	133 7 8-			545.3		
		XTHICK	•				
77	L				71.5	56.3	38.3
23	L				33664		
24	1		AX THICK	WE 22	37.3	l	
?	1	1	•	<u>i</u>	194.0	32.6	
ζ c	•		AX THICK	WE22	13.6		
27	MEAN AERODYNAMIC CHORD I	THE LENG	JECTEDI		370.5		
2 8	L.E. OF M. A.C. TF.S.I				1524.55	2845.2	
₹:	1		1		• •		153.0
31.		<u>בצרסדיטאו</u>	* MAC V	PATE !	FTT	1	113.5
11					1		
3.5	AREAS ISO FTI	LE SEATS		SPCILERS		ELEVATRS	256.7
3.		TE FL APS	351.7	ATLERENS	25208	RJUDERS	226.7
34			 				
1	ALIGHTING GEAR	 		:		MAIN	YUSE
? 6	LENSTH - OLSO EXTENDED	- C.L. A	XEE TO C	L. TRUN	NICHTINI	81.5	55.1
3	DUED TRAVEL - FULL EXT					25.0	i
J.		 	}	 		ट्रव	4
3		 	 	1		24	
ग			 			1	
	I MANACH OF SINGIS	L	•	1	l	1	
רקו	1	Y TOALLON	S ::-	282-0		4	
	TYDRAULIC SYSTEM CAPACIT	YTGACCOV	51 :	282-0	11.		
	TYDRAUCIC SYSTEM CAPACIT	YTGALLOY	57:	282.0		NC. IKS.	GAL . UNPI
य है य इ	FUEL - INTERNAL	YTGALLON	57. 3	282-0			GAL.UNP1
य है य द	TYDRAUCIC SYSTEM CAPACIT FUEC AND CORE SYSTEM FUEL - INTERNAL OIL					NC. IKS.	GAL . UNPT
य द य द य द	TYDRAUCIC SYSTEM CAPACIT FUEC AND CUBE SYSTEM FUEC - INTERNAC OIL HURIZUNTAL REFERENCE DAT	UT TO FIS	. 2ER C	IN) 0		NC. IKS.	GAL.UNP1
4 2 4 3 4 3 4 6	TYDRAUCIC SYSTEM CAPACIT FUEL AND CURE SYSTEM FUEL - INTERNAL OIL HORIZONTAL REFERENCE DAT VERTICAL REFERENCE DATUM	U1 10 F-5	. 2ER C	IN) 0		NC. IKS.	GAL.UNPT
य द य द य द य द य द य द	TYDRAULIC SYSTEM CAPACIT FUEL AND LURE SYSTEM FUEL - INTERNAL OIL HORIZONTAL REFERENCE DAT VERTICAL REFERENCE DATUM 7 STRUCTUMAL DATA - CONDIT	U1 10 F-5	. 2ER C	IN) 0	FUEL AT	NC. TKS.	GAL.UNPT 43000 43
य द य द य द य द य द य द	TYDRAULIC SYSTEM CAPACIT FUEL AND LUCE SYSTEM FUEL - INTERNAL OIL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM 7 STRUCTUMAL DATA - CONDITE FLIGHT	U1 10 F-5	. 2ER C	IN) 0	FUE: 11	NC. 1K5. 12 4 51 RES 50A 72 ECTIC	GAC.UNPT 13UPU 13 ULT LF
य है य दे य दे य दे य दे य दे य दे य दे य दे	TYDRAULIC SYSTEM CAPACIT FUEL AND LOVE SYSTEM FUEL - INTERNAL OIL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM 7 STRUCTUM AL DATA - CONDIT B FLIGHT 3 LANDING	UT TO F.S	. 2ER C	IN) 0	FUE: AT	NC. TKS. 12 4 51 RES SUM 72 ECTOR	GAC.UNPT 73000 73 0CT LF 2.72
य है। य दे य दे य दे य दे य दे य दे य दे य दे	TYDRAULIC SYSTEM CAPACIT FUEL - AND CORE SYSTEM FUEL - INTERNAL OIL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM 7 STRUCTUMAL DATA - CONDIT B FLIGHT 3 LANDING 1 MAXIMUM CESIGN GROSS W	UT TO F.S	ZERC IIN	13 E:	FUE: 11	NC. TKS. 12 4 51 RES SGA 72 ECTT 53 5 8 5 CTT 63 5 6 5 CTT	GAC.UNPT 73000 73 001 LF 2.72 2.110
42 43 43 41 41 41 15 15 15 15 15 15 15 15 15 15 15 15 15	TYDRAULIC SYSTEM CAPACIT FUEL - AND LUEE SYSTEM FUEL - INTERNAL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM T STRUCTURAL DATA - CONDIT B FLIGHT L ANDING KAXIMUM CESIGN GROSS W	UT TO F.S	ZERC IIN	13 E:	FUE: #1 TEAU96 V 6 94 6 Tenti96	72 ELLE 15 20 20 20 20 20 20 20 20 20 20 20 20 20	GAC.UNPT 73000 73 0CT LF 3.72 3.28
42 44 46 46 47 47 47 47 47 47 47 47 47 47 47 47 47	TYDRAULIC SYSTEM CAPACIT FUEL - INTERNAL OIL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM T STRUCTURAL DATA - CONDIT B FLIGHT L ANDING KAXIMUM CESIGN GROSS W HURIKUM FLYING WEIGHT W	UT TO F.S. TO WILL TON ETGHT TH ZERO	ZERC IN	13 E:	FUE: 21 TEAU96 VE 346 TENU96	NC. TKS. 12 4 51 RES SON 72 ECTO 12 90 90 90 90 90 90 90 90 90 90 90 90 90	GAC.UNPT 43 43 UCT LF 3.7: 2.10 3.38
पार पार के किया है। पार पार की जिल्ला के किया के किया के किया किया किया किया किया किया किया किया	TYDRAULIC SYSTEM CAPACIT FUEL - AND CUEE SYSTEM FUEL - INTERNAL HURIZUNTAL REFERENCE DATUM VERTICAL REFERENCE DATUM STRUCTURAL DATA - CONDIT FLIGHT LANDING KAXIMUM CESIGN GROSS W HAXIMUM GROSS WEIGHT W HIRIKUM FLYING HEIGHT LIMIT CANDING SINKING	UT TO F.S TO WILL TON ETGHT TH ZERO	ZERC IN ZERG IN WING FUL VISECI	[N) (:	FUE: AT TEAU96 % 6 946 1 2000 96 9 211	72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON 72 TRES SON	GAC.UNPT 43 OLT LF 5.7: 2.10 3.2: 3.3: 2.7:
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पार्थ । पार्थ ।	TYDRAULIC SYSTEM CAPACIT FUEL AND CURE SYSTEM OIL HURIZUNTAL REFERENCE DAT VERTICAL REFERENCE DATUM STRUCTURAL DATA - CONDIT B FLIGHT CANDING MAXIKUM CESIGN GROSS W MAXIKUM CESIGN GROSS W MAXIKUM FLYING WEIGHT WING LIFT ASSUMED FOR STALL SPEEC - LANDING	EIGHT TH ZERO SPEED IF LANDING TOWN	ZERC IIN ZERG IIN ZERG IIN ZERG IIN ZING FUE ZINGEN CI ATTO:N=2-CX ZION-PRES	INI O II S NOTTICNT IET CFF IS OIFFER	FUE _ AT	NC. TKS. 12 4 51 RES SGN 72 ECTO 52 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9	GAC.UNPT 43 UCT LF 3.7: 3.39 2.7: 2.113 111
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				TABI	TABLE 8						
	C-5A	GROSS WEIGHT		BALANCE AND		INERTIA	SUZZARY				
ROILICKOO LEDIEM SSOED	TEOLEN		₽%			SERONI	ı,	1, Y	° r	Ixz	*
(LEIDING GEAR DOAN)	(LLB)	F.S.	MAC	В.Г.	W.L.	nanc#_ Letac	(Lb-In_{x}^{2})	$(Lb-In^2)$ x 10^{-6})	$(Lb-In^2_{\times 10^{-6}})$	$(1b-10^2)$ x 10^{-6}	ю
Weight Empty	325,263	1400	39.3	1	252	63	57,478.5	6.095,66	145,183.5	10,721.4 6.87	6.87
Basic Weight Plus Troop Kit	355,537	1405	40.7	-	254	61	57,863.4	101,742.1	57,863.4 101,742.1 147,586.2	11,043.8 6.91	6.91
Operating Weight	729,452	1393	37.5		252	63	57,909.0	101,485.9	57,909.0 101,485.9 146,945.8	10,697.5 6.76	92.9
Operating Weight & Troop Kit	357,033	1405	39.9	H	254	61	61,66,75	102,999.2	57,991.9 102,999.2 148,411.1	10,951.2 6.81	6.81
Basic Flight Design-Fax.Cargo	728,000	1357	27.7	0	250	65	150,214.2	150,202.6	50,214.2 150,202.6 283,950.9	12,051.6 5.11	5,11
Baric Flight Design-Yax. Fuel	728,000	1379	33.7	0	526	39	170,866.5	124,743.5	170,866.5 124,743.5 279,748.2	10,618.1 5.52	5.52
Manual Design-Maximum Cargo	769,000	1350	25.8	0	246	69	149,599.9	158,894.7	149,599.9 158,894.7 291,557.5	12,522.0 4.92	1.92
Manigum Design-Maxigum Puel	200,000	1371	31.5	0	271	477	171,415.7	171,415.7 133,034.9	287,845.4	11,064.1	5.38
Ferry Mission (Zero Cargo)	655,533	1393	37.5	٥	285	30	169,830.5	109,899.6	169,830.5 109,899.6 265,343.4	9,741.7 5.76	5.76
Institutione Landing (Max. Cargo) 635,850	635,850	13:11	23.4	0	232	83	91,010.0	154,948.7	91,010.0 154,948.7 230,269.2	12,272.7 5.00	5.00
Personnel/Fayload	728,000	1370	31.2	0	253	62	150,180.0	151,885.0	[50,180.0 151,885.0 285,509.5	11,974.0 5.02	5.02
Tyrical Vehicle	7:28,000	1333	34.8	0	249	99	149,575.0	151,391.6	149,575.0 151,391.6 285,070.4	10,991.5 4.61	1.61
XAC Passenger	728,000	1369	31.0	0	506	64	166,248.6	.66,248.6 151,574.2	301,287.4	12,191.9	5.12
** Fost Forward C.G.	713,904	1339	22.9	0	549	99	139,966.0	152,015.6	159,966.0 152,015.6 275,469.4	12,351.7	5.17
*** East Aft C.G. (Gear Up)	683,904	1406	41.0	0	246	69	135,513.4	145,574.8	135,513.4 145,574.8 265,053.0 10,261.4 4.50	10,261.4	4.50

Angle of Inclination of the principal axis (nose down) with respect to the air vehicle "x" axis.

Represents the most critical forward center of gravity condition with respect to the allowable center of gravity limits for the 2.5g maximum cargo mission.

Represents the most critical aft center of gravity condition with respect to the allowable center of gravity limits for the 2.5g maximum cargo mission.

The weights have been reallocated for inertia calculation as shown in Table 9, and pertinent geometry items are given in Table 10.

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Table 9
Reallocated Weights

WING GROUP	WEIGHT	X,Y,Z(when needed)
Structure	82045	
Surface Controls	3796	
Fuel System	2458	
Anti-Ice	229	
Trapped Fuel	562	
Total	89090	
FUSELAGE GROUP		
7 0 0 11 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		
Structure	116048	
Distributed:		
Surface Control	1270	
Inst. & Navi.	281	
Hydraulic	2666	
Electrical	2761	
Total Dist.	6978	
POINT MASSES:		
Main Landing Gear	33681	1292,264,81
Nose Landing Gear	4407	418,0,86
Auxiliary Power Unit	933	1485,264,141
Air Conditioning	3411	964,0,294
Auxiliary Gear	39	2025,0,308
Crew	1290	318,0,332

Table 9 (cont'd)

Radar	WEIGHT 376	$\frac{X,Y,Z}{80,0,260}$
Surface Controls	271	290,0,332
Instruments & Navig	ation657	290,0,332
Other Equipment	0	
Tiedown Devices	1750	694,0,165
Life Rafts	200	698,0,334
Food	17	690,0,335
Water	43	601,0,365
Liquid 0 ₂	63	1280,0,153
Total Pt. Ma	uss 47138	
Volumes:		
Avionics	3514	707,0,316
Furnishings	6836	763,0,281
Total Vol	L0350	
HORIZONTAL TAIL GRO	OUP	
Structure	6793	
Surface Controls	913	
Total	7706	
VERTICAL TALL GROU	P	
Structure	5603	•
Surface Control	885	
Total	6488	
PROPULSION GROUP		
Engines & System	33804	
Hydraulic	1313	

Table 9. Continued

690
264
9586
45657

Aircraft WE

Table 10. C-5A Geometry Definitions for Inertia

GEOMETRY DATA

The state of the s

WING	HORIZ	VERT
Λ _{L1} - 28°	30°	37 ^o
Λ _T - 14°	9 ⁰	30°
b - 1336	412	405
c - 525	250	371
t _r - 72	26	48
t _t - 20	10	39
XS4 - 806	2605	2425
ZS1 - 370	780	365
YS4 - 0	0	0
05°	-5°	90°
FUSELAGE	PROPULSION	
1 _h - 440	R _e - 80	
1 _c - 1300	1 _e - 312	
1 _t - 1027	$XP_1 - 1020 \qquad XP_2 - 1165$	
R - 138	$YP_1 - 476 \qquad YP_2 - 743$	
z _b - 260	$ZP_1 - 222 ZP_2 - 198$	
ADDITIONAL ITEMS		
A, 3 - 27°	t _{f0} - 14 1 _p - 1600	

A. Centroids

WING

$$C_a = 525 C_b = 710 C_c = 858$$

USING Eq
$$(8)*$$
, XS1 = 422

USING Eq (9),
$$YS^1 = 441$$
 $YS^1 = YS^1 \cos(-5^0) = 440$

$$ZS3 = YS1 \sin (-5^{\circ}) = -38$$

HORIZONTAL

$$C_a = 238 C_b = 250 C_c = 315$$

USING Eq
$$(8)$$
, XS1 = 165

USING Eq (9), YS1 = 144
$$\frac{1}{4}$$
 YS1 = YS1 cos (-5°) = 143.5

$$ZS3 = YS1 \sin (-5^{\circ}) = -13$$

VERTICAL

$$C_a = 305 C_b = 371 C_c = 605$$

USING Eq
$$(8)$$
, XS1 = 277

USING Eq (9), YS1 = 188
$$YS1 = YS1 \cos 90^{\circ} = 0$$

$$ZS3 = YS1 \sin 90^{\circ} = 188$$

WING FUEL TANK

USING Eq (59) XF1 = 254

USING Eq (60) YF1 = 323 YF1 = YF1
$$\cos (-5) = 321.6$$

$$ZF2 = YF1 \sin (-5) = -28$$

B. Wing Group Inertia

USING Eq (1),
$$I_{1x} = 2.7028033 \times 10^{10}$$

USING Eq (2),
$$I_{1y} = 1.9574734 \times 10^{10}$$

USING Eq (3),
$$I_{1z} = 4.6602767 \times 10^{10}$$

TRUE
$$I_{1y} = I_{1y} \cos(-5) + I_{1z} \sin(-5) = 1.5438548 \times 10^{10}$$

TRUE $I_{1z} = I_{1y} \sin (-5) + I_{1z} \cos (-5) = 4.471938 \times 10^{10}$ USING (7), $I_{1xz} = -1.819266687 \times 10_9$ $I_x = I_{1x} - 89090 (440)^2 - 89090 (-38)^2 + 89090 (440 + 0)^2$ $+ 89090 (-38 + 370)^2 = 3.67192431 \times 10^{10}$ $I_y = I_{1y} - 89090 (422)^2 - 89090 (-38)^2 + 89090 (422 + 806)^2$ $+ 89090 (-38 + 370)^2 = 1.4361055 \times 10^{11}$ $I_z = I_{1z} - 89090 [(422)^2 + (440)^2] + 89090 (422 + 806)^2$ $+ 89090 (440 + 0)^2 = 1.63200171 \times 10^{11}$ $I_{xz} = I_{1xz} - 89090 (422) (-38) + 89090 (422 + 806) (-38 + 370) = 3.5931017 \times 10^{10}$

C. HORIZONTAL TAIL GROUP INERTIA

USING (1), $I_{1x} = 2.45844912 \times 10^8$

USING (2), $I_{1y} = 2.80151979 \times 10^8$

USING (3), $I_{1z} = 5.2599689 \times 10^8$

TRUE $I_{1y} = I_{1y} \cos (-5) + I_{1z} \sin (-5) = 2.3324227 \times 10^8$

TRUE $I_{1z} = I_{1y} \sin (-5) + I_{1z} \cos (-5) = 4.9957846 \times 10^8$

USING (7), I_{1xz}^{-} -1.941127 x 10⁷

 $I_x = I_{1x} - 7706 (143.5)^2 - 7706 (-13)^2 + 7706 (143.5 + 0)^2 + 7706 (-13 + 780)^2 = 4.77784763 \times 10^9$

 $I_{y} = I_{1y} - 7706 (165)^{2} - 7706 (-13)^{2} + 7706 (165 + 2605)^{2}$

 $+ 7706 (-13 + 780)^2 = 6.3682867 \times 10^{10}$

 $I_z = I_{1z} - 7706 (165^2 + 143.5^2) + 7706 (165 + 2605)^2 + 7706 (143.5 + 0)^2$ = 5.82546306 x 10¹⁰

 $I_{xz} = I_{xz} - 7706(165) (-13) + 7706(165 + 2605) (-13 + 780) = 1.636920864 \times 10^{10}$

D. VERTICAL TAIL GROUP INERTIA

USING (1), I_{1x} = 3.17905191 x 10⁸

USING (2), $I_{1y} = 7.2770685 \times 10^8$

USING (3),
$$I_{1z} = 1.045612041 \times 10^9$$

TRUE $I_{1y} \approx I_{1y} \cos 90 + I_{1z} \sin 90 = 1.045612041 \times 10^9$
TRUE $I_{1z} = I_{1y} \sin 90 + I_{1z} \cos 90 = 7.2770685 \times 10^8$
USING (7), $I_{1xz} = 2.58157 \times 10^8$
 $I_x = I_{1x} - 6488 (0)^2 - 6488 (188)^2 + 6488 (0 + 0)^2 + 6488 (188 + 365)^2$
 $= 2.07268211 \times 10^9$
 $I_y = I_{1y} - 6488 (277)^2 - 6488 (188)^2 + 6488 (277 + 2425)^2 + 6488 (188 + 365)^2$
 $= 4.967018756 \times 10^{10}$
 $I_z = I_{1z} - 6488 [(277)^2 + 0^2] + 6488 (277 + 2425)^2 + 6488 (0 + 0)^2$
 $= 4.75975055 \times 10^{10}$

$I_{xz} = I_{1xz} - 6488 (277)(188) + 6488(277 + 2425)(188 + 365) = 9.69440853 \times 10^9$

STRUCTURE:

E. FUSELAGE GROUP INERTIA

$$S_n = \pi (138)$$
 $\sqrt{138^2 + 440^2} = 199,920$
 $S_c = 2 \pi (138)(1300) = 1,127,203$
 $S_t = \pi (138)$ $\sqrt{138^2 + 1027} = 449,247$
 $S_c = 1,776,370$

$$W_n = \frac{199,920}{1,776,370}$$
 (116,048) = 13,061

$$W_{c} = \frac{1,127,203}{1,776,370}$$
 (116,048) = 73,639

$$W_t = \frac{449,247}{1,776,370}$$
 (116,048) = 29,349

USING (25),
$$I_x = 9.651054 \times 10^9$$

USING (26),
$$I_y = 2.36853866 \times 10^{11}$$

USING (27),
$$I_z = 2.290090211 \times 10^{11}$$

USING (28),
$$I_{xz} = 3.722851418 \times 10^{10}$$

DISTRIBUTED CONTENTS:

USING (29),
$$I_x = 6.04602 \times 10^8$$

USING (30),
$$I_v = 1.79106443 \times 10^{10}$$

USING (31),
$$I_z = 1.743893 \times 10^{10}$$

USING (32),
$$I_{xz} = 2.6135712 \times 10^9$$

VOLUMES:

AVIONICS: RECTANGULAR SOLID

USING (37),
$$I_x = \frac{3514}{12} (250^2 + 250^2) + 3514 (316)^2$$

$$= 3.8749815 \times 10^8$$

USING (38),
$$I_y = \frac{3514}{12} (250^2 + 1315^2) + 3514 (707^2 + 316^2)$$

$$= 2.6320402 \times 10^9$$

USING (39),
$$I_z = \frac{3514}{12} (1315^2 + 250^2) + 3514 (707)^2$$

$$= 2.2811462 \times 10^9$$

USING (40),
$$I_{xz} = 3514 (707)(316) = 7.850698 \times 10^8$$

FURNISHINGS: RECTANGULAR SOLID

USING (37),
$$I_x = \frac{6836}{12} (250^2 + 250^2) + 6836 (281^2)$$

USING (38),
$$I_y = \frac{6836}{12} (250^2 + 1100^2) + 6836 (763^2 + 281^2)$$

USING (39),
$$I_z = \frac{12}{6836} (1100^2 + 250^2) + 6836 (763^2)$$

USING (40),
$$I_{xz} = 6836 (763)(281) = 1.4656589 \times 10^9$$

$$33681 (1292^2 + 81^2)$$

$$4407 (418^2 + 86^2)$$

933
$$(1485^2 + 141^2)$$

$$3411 (964^2 + 294^2)$$

+ 2
$$(11, 414.3)$$
 $(3(80)^2 + 312^2) + 11,414.3 (1165^2 + 743^2)$
= 7.29527635 x 1010

USING (48), $I_{xz} = 22829(1020)(222) + 22829(1165)(198) = 1.043536419 \times 10^{10}$

G. SUMMATION OF GROUP I x,y,z

Total $I_x = 7.817685768 \times 10^{10}$

Total $I_y = 6.5382519 \times 10^{11}$

Total $I_z = 6.59099235 \times 10^{11}$

Total $I_{xz} = 1.198992973 \times 10^{11}$

H. AIRCRAFT CENTER OF GRAVITY

 \bar{X} : W (X)

Wing

89,090 (1228)

Fuselage

13,061 (293)

73,639 (1090)

29,349 (2082)

6978 (1423)

Horizontal Tail

7706 (2770)

Vertical Tail

6488 (2702)

Propulsion

22,829 (1020)

22,829 (1165)

Point Masses

33681 (1292)

4407 (418)

933 (1485)

3411 (964)

Volumes

$$WX = 4.13282587 \times 10^8$$

$$W = 329,456$$

$$\bar{X} = \frac{WX}{W} = 1254.4$$

Fuselage

Wing

89,090 (332)

Horizontal Tail

7706 (767)

Vertical Tail

6488 (553)

Propulsion

22,829 (222)

22,829 (198)

Point Masses

- 33,681 (81)
- 4,407 (86)
 - 933 (141)
 - 3411 (294)
 - 39 (308)
- 1290 (332)
- 376 (260)
- 271 (332)
- 657 (332)
- 1750 (165)
- 200 (334)
- 17 (335)
- 43 (365)
- 63 (153)

Volumes

- 3514 (316)
- 6836 (281)
- Σ WZ = 8.9156803 x 10⁷
- $\Sigma W = 329,456$
- $\frac{\Sigma WZ}{\Sigma W} = 270.6$
- I. MOMENTS OF INERTIA ABOUT AIRCRAFT CENTER OF GRAVITY (OPERATING WEIGHT EMPTY)
- $I_{cgx} = I_x (329,456) (270.6)^2$ = 5.40461473 x 10¹⁰

$$I_{cgy} = I_y - 329,456 (270.6^2 + 1254.4)^2$$

$$= 9.88529;998 \times 10^{10}$$

$$I_{cgz} = I_z - 329,456 (1254.4)^2$$

$$= 1.406938403 \times 10^{11}$$

$$I_{cgyz} = 8.06854177 \times 10^9$$

J. CALCULATIONS FOR BASIC FLIGHT DESIGN WEIGHT WITH MAX FUEL: INTERNAL WING FUEL:

USING (53),
$$I_{4x} = 5.24631042 \times 10^{10}$$

USING (54), $I_{4y} = 2.467113514 \times 10^{10}$
USING (55), $I_{4z} = 7.71342393 \times 10^{10}$

USING (58),
$$I_{4xz} = -2.95088621 \times 10^9$$

TRUE
$$I_{4y} = I_{4y} \cos (-5) + I_{4z} \sin (-5) = 1.7854562 \times 10^{10}$$

TRUE $I_{4z} = I_{4z} \sin (-5) + I_{4z} \cos (-5) = 734690489 \times 10^{10}$

$$I_x = I_{4x} - 318500 (321.6)^2 - 318500 (-28)^2 + 318500 (321.6 + 190)^2 + 318500 (-28 + 360)^2 = 1.3774084 x 10^{11}$$

$$I_y = I_{4y} -318500 (254)^2 - 318500 (-28)^2 + 318500 (254 + 941)^2$$

$$= 4.869888185 \times 10^{11}$$

$$I_z = I_{4z} - 318500 (254^2 + 321.6^2) + 381500 (254 + 941)^2 + 318500 (321.6 + 190)^2$$

$$I_{xz} = I_{4xz} -318500 (254) (-28) + 318500 (254 + 941) (-28 + 360)$$

= 1.25665746 x 10¹¹

PAYLOAD

USING (69),
$$I_x = \frac{71787}{(12)(170^2 + 170^2) + 71787(192)^2} = 2.99213002 \times 10^9$$
USING (70), $I_y = \frac{71787}{12}(1600^2 + 170^2) + 71787(1084^2 + 192^2)$

= 1.0248755

USING (71),
$$I_z = \frac{71787}{12} (1600^2 + 170^2) + 71787 (1084)^2 = 9.98411921 \times 10^{10}$$

USING (72),
$$I_{xz} = 71787 (1084) (192) = 1.494088474 x $10^{10}$$$

POINT MASSES:

$$680 (440^2 + 319^2)$$

7581
$$(1619^2 + 341^2)$$

$$I_v = 2.09534 \times 10^{10}$$

$$I_z = 2.000267 \times 10^{10}$$

$$W_{pc} = 8261$$

$$I_x = \frac{8261 (180)^2}{2} + 8261 (335)^2 = 1.0609189 \times 10^9$$

$$I_{xz} = 4.2807557 \times 10^9$$

Total
$$I_x = 2.199674956 \times 10^{11}$$

Total
$$I_y = 1.25181229 \times 10^{12}$$

Total $I_z = 1.340776051 \times 10^{12}$

Total $I_{xz} = 2.647866836 \times 10^{11}$

NEW CENTER OF GRAVITY DUE TO ADDITIONAL WEIGHT:

 \bar{x} : 318500 (1195)

71787 (1084)

680 (440)

7581 (1619)

EWX (INCLUDING OPERATING WEIGHT) = 8.84280034×10^8

ΣW (INCLUDING OPERATING WEIGHT) = 728,025

 $\bar{x} = 1214.6$

 \bar{z} : 318500 (332)

71787 (192)

680 (319)

7581 (341)

ΣWZ (INCLUDING OPERATING WEIGHT)= 2.114839 x 10⁸

EW (INCLUDING OPERATING WEIGHT) = 728,025

 $\overline{Z} = 290$

MOMENTS OF INERTIA ABOUT AIRCRAFT CENTER OF GRAVITY:

$$I_{cgx} = I_{x} - 728025 (290)^{2} = 1.5874059 \times 10^{11}$$

$$I_{cgy} = I_y - 728025 (290.^2 + 1214.6^2) = 1.16564203 \times 10^{11}$$

$$t_{cgz} = I_z - 728025 (1214.6)^2 = 2.66754869 \times 10^{11}$$

$$I_{cgxz} = I_{xz} - 728025$$
 (290) (1214.6) = 8.3515259 x 10⁹

SUMMARY OF ACTUAL VERSUS CALCULATED INERTIAS FOR C-5A (MOMENTS OF INERTIA \times 10^{-6})

マス・アイン (1995年) (1995年)

		I (ROLL)			I (PITCH))
	ACTUAL	CALCULATED	% ERROR	ACTUAL	CALCULATED	% ERROR
OPERATING WEIGHT EMPTY	57,909	54,246	6.3	101,486	98,853	2.6
WITH MAX FUEL	170,867	158,941	7.0	124,744	116,564	6.6
		I (YAW)			I _{xz}	
	ACTUAL	I _z (YAW)	% ERROR	ACTUAL	I _{xz}	% ERROR
OPERATING WEIGHT EMPTY	ACTUAL 146,944		2 ERROR 4.3	ACTUAL 10,968	I _{XZ} CALCULATED 8068	% ERROR 26.4

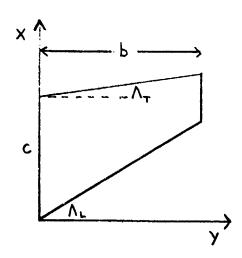
References

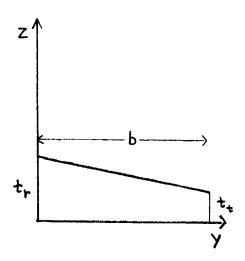
- 1. USAF Stability and Control Datcom, Douglas Aircraft Division, October 1960.
- 1. Interactive Computer-Aided Design Aircraft Flying Qualities Program, ASD/XR 74-17, August 1974.
- 3. C-5A Actual Weight and Balance Report, Lockheed
- 4. F-15A Actual Weight Report, McDonnell Douglas MDC A3154, January 1975.
- 5. A-10A Actual Weight and Balance Report, Fairchild SW160 R0070
- 6. B-52G Actual Weight and Balance Report, Boeing D3-4586, August 1962

Appendix - Derivation of Equations

1. Surface Inertia and Volume

(Surface Diagram)





$$I = \int r^{2} dm, \quad dm = \rho dV, \quad I = \rho \int r^{2} dV, \quad dV = t dx dy$$

$$I_{IX} (ROLL) = \rho \int_{0}^{b} \int_{y \tan \Lambda_{L}}^{c + y \tan \Lambda_{T}} y^{2} \left(t_{r} - \frac{t_{r} - t_{r}}{b}, y \right) dx dy$$

$$= \rho \int_{0}^{b} \left(y^{2}c + y^{3} \tan \Lambda_{T} - y^{3} \tan \Lambda_{L} \right) \left(t_{r} - \frac{t_{r} - t_{r}}{b}, y \right) dy$$

$$= \frac{Wb^{3}}{V} \left\{ \left[\left(t_{r} - t_{r} \right) \left(\frac{c}{4} + \frac{b \tan \Lambda_{T}}{5} - \frac{b \tan \Lambda_{L}}{5} \right) \right] + \left[t_{r} \left(\frac{c}{3} + \frac{b \tan \Lambda_{T}}{4} - \frac{b \tan \Lambda_{L}}{3} \right) \right] \right\}$$

Calculating the volume (v):

$$V = \int \int \int dx dy dz = \int_{0}^{b} \int_{y + an \Lambda_{L}}^{c + y + an \Lambda_{T}} (t_{t} - \frac{t_{t} - t_{t}}{b} y) dxdy$$

$$= \int_{0}^{b} \left[c + \gamma tan \Lambda_{\tau} - \gamma tan \Lambda_{L} \right] \left[t_{\tau} - \frac{t_{\tau} - t_{\tau}}{b} y \right] dy$$

$$= b \left\{ t_{\tau} \left[c + \frac{b}{2} \left(tan \Lambda_{\tau} - tan \Lambda_{L} \right) \right] - \left(t_{\tau} - t_{t} \right) \left[\frac{c}{2} + \frac{b}{3} \left(tan \Lambda_{\tau} - tan \Lambda_{L} \right) \right] \right\}$$

$$I_{1y} \left(P_{1TCH} \right) = P \int_{0}^{b} \int_{0}^{c+\gamma tan \Lambda_{\tau}} x^{2} \left(t_{\tau} - \frac{t_{\tau} - t_{\tau}}{b} y \right) dx dy$$

$$= P \int_{0}^{b} \left\{ \frac{\left(c + \gamma tan \Lambda_{\tau} \right)^{3}}{3} \left(t_{\tau} - \frac{t_{\tau} - t_{t}}{b} y \right) - \frac{\gamma^{3} tan^{3} \Lambda_{L}}{3} \left(t_{\tau} - \frac{t_{\tau} - t_{t}}{b} y \right) \right\} dy$$

$$= P \int_{0}^{b} \left\{ \left[\left(- \frac{t_{\tau} - t_{\tau}}{b} \right) \left(\frac{c^{3} \gamma}{3} + c^{2} \gamma^{3} tan \Lambda_{\tau} + c \gamma^{3} tan^{2} \Lambda_{\tau} \right) \right.$$

$$+ \frac{\gamma^{4} tan^{3} \Lambda_{\tau}}{3} - \frac{\gamma^{4} tan^{3} \Lambda_{L}}{3} \right] + \left[t_{\tau} \left(\frac{c^{3}}{3} + c^{2} \gamma tan \Lambda_{\tau} + c \gamma^{3} tan^{2} \Lambda_{\tau} \right) \right]$$

$$= \frac{Wb}{V} \left\{ \left[t_{\tau} \left(\frac{c^{3}}{3} + bc tan \Lambda_{\tau} \left(\frac{c}{2} + \frac{btan \Lambda_{\tau}}{3} \right) + \frac{b^{3}}{12} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{Wb}{V} \left\{ \left[t_{\tau} \left(\frac{c^{3}}{3} + bc tan \Lambda_{\tau} \left(\frac{c^{3}}{6} + bc tan \Lambda_{\tau} \left(\frac{c}{3} + \frac{btan \Lambda_{\tau}}{4} \right) + \frac{b^{3}}{12} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$= \frac{b}{V} \left\{ \left[t_{\tau} \left(tan^{3} \Lambda_{\tau} - tan^{3} \Lambda_{L} \right) \right] \right\}$$

$$I_{1xz} = \rho$$

$$\int_{0}^{b \sin \theta} \int_{\frac{z \tan \Lambda_{1}}{\sin \theta}}^{crt} xzt \sin \theta \, dxdz + \frac{z \tan \Lambda_{1}}{\sin \theta}$$

$$\frac{z \tan \Lambda_{1}}{\sin \theta}$$

$$= t_{r} \rho$$

$$\int_{0}^{b \sin \theta} \int_{\frac{z \tan \Lambda_{1}}{\sin \theta}}^{crt} xzt \cos \theta \, dxdy + \frac{z \tan \Lambda_{1}}{\cos \theta}$$

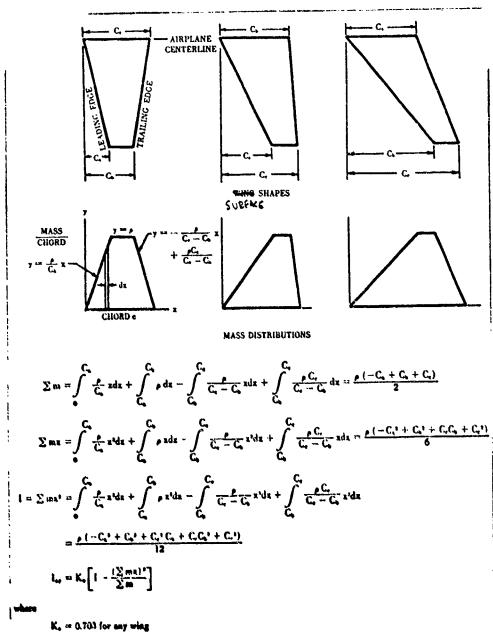
$$\frac{z \tan \Lambda_{1}}{\sin \theta}$$

$$\int_{\frac{z \tan \Lambda_{1}}{\cos \theta}}^{crt} xz \sin \theta \, dxdz + t_{r} \rho$$

$$\int_{0}^{b \cos \theta} \int_{\frac{z \tan \Lambda_{1}}{\sin \theta}}^{crt} xz \cos \theta \, dxdy - \frac{\rho}{\rho} (t_{r} - t_{e}) \int_{\frac{z \tan \Lambda_{1}}{\sin \theta}}^{crt} \int_{0}^{b \sin \theta} xz^{2} \, dzdx$$

$$- \frac{\rho}{\rho} (t_{r} - t_{e}) \int_{0}^{b \cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\sin \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\sin \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\cos \theta} \int_{0}^{crt} \frac{y \tan \Lambda_{1}}{\sin$$

2. Longitudinal and spanwise surface center of gravity location Longitudinal centroid:



K. = 0.703 for any wing

K. = 0.771 for any horizontal or vertical stabilizer

Assuming that $I_{oy} = K_o I - K_o \frac{(EMX)^2}{EM}$ and knowing that $\frac{\pi}{x} = \frac{EMX}{EM}$

We have $I_{ov} = K_o I - \Sigma M K_o \bar{x}$. Since \bar{x} is multiplied by K_o we assume that \bar{x} is multiplied by $\sqrt{K_0}$ $\bar{x} = \frac{2\rho (-c_a^2 + c_b^2 + c_c c_b + c_c^2)}{(-c_a + c_b + c_c)}$

$$x = (-c_a^2 + c_b^2 + c_c^2 + c_c^2) \sqrt{(K_0)}$$

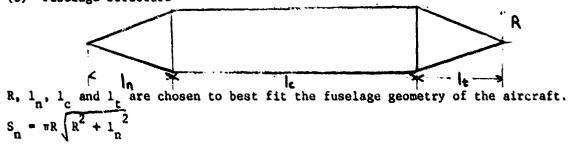
(Where $\bar{x} = XS1$, XS2, or XS3)

Spanwise centroid:

THE BUTTON IN THE

Using diagram in Section (1) we have:

(3) Fuselage Structure



$$S_{n} = \pi R \sqrt{R^{2} + 1_{n}^{2}}$$

$$S_c = 2\pi R \frac{1}{c}$$
 $S_t = \pi R \sqrt{R^2 + 1_t^2}$

Distributing weight according to surface area:

$$\frac{W_n - S_n (W_g)}{S_n + S_c + S_c}$$

$$\frac{W_{c} - S_{c} (W_{s})}{S_{n} + S_{c} + S_{t}}$$

$$W_{t} = S_{t} (W_{s})$$

$$S_{n} + S_{c} + S_{t}$$

(4) Fuselage distributed contents

 I_{o} for a right - cylindrical open ended shell is given in Section 9.

Translating this and defining the terms in different notation:

$$I_{x} = W_{dc} R^{2} + W_{dc} (Z_{b})^{2}$$

$$I_{y} = \frac{W_{dc}}{2} [R^{2} + \frac{1}{6} (XS4 - CREW c.g.)^{2}] + W_{dc} (XS4 - CREW c.g. + CREW c.g.)^{2}$$

$$CREW c.g.)^{2} + W_{dc} (Z_{b})^{2}$$

$$I_{z} = I_{y} - W_{dc} (Z_{b})^{2}$$

(5) Fuselage volumes of mass

 I_{o} for a right circular shell and solid rectangle are given in Section 9.

Translating these to the remote axes and changing the notation gives:

Right circular cylinderical shell

$$I_{x} = W_{vo} R_{v}^{2} + W_{vo} (z)^{2}$$

$$I_{y} = \frac{W_{vo}}{2} (R_{v}^{2} + \frac{1}{2} + W_{vo} (x^{2} + z^{2}))$$

$$I_{z} = \frac{W_{vo}}{2} (R_{v}^{2} + \frac{1}{2} + W_{vo} (x^{2} + z^{2}))$$

Rectangular solid:

$$I_{x} = \frac{W_{vo}}{\frac{12}{12}} (2R_{v}^{2} + 2R_{v}^{2}) + W_{vo} (z)^{2}$$

$$I_{y} = \frac{W_{vo}}{\frac{12}{2}} (1_{v}^{2} + 2R_{v}^{2}) + W_{vo} (x^{2} + z^{2})$$

$$I_{z} = \frac{W_{vo}}{\frac{12}{12}} (1_{v}^{2} + 2R_{v}^{2}) + W_{vo} (x)^{2}$$

(6) Fuselage point masses

For point masses, the inertia about the center of the mass is so small that it can be neglected. For pitch and yaw we just translate the mass to each respective axis:

$$I_x = W_p (y^2 + z^2)$$
 $I_y = W_p (x^2 + z^2)$
 $I_z = W_p (x)^2$

$$I_{y \text{ nose}} = \frac{W_{n}}{4} (R^{2} + \frac{2}{9} I_{n}^{2}) + W_{n} (\frac{2}{3} I_{n})^{2} = \frac{W_{n}}{4} (R^{2} + 2I_{n}^{2})$$

$$I_{y \text{ cylinder}} = \frac{W_{c}}{2} (R^{2} + \frac{1}{c^{2}}) + W_{c} (\frac{1}{2} I_{c} + I_{n})^{2} = \frac{W_{c}}{2} (R^{2} + \frac{1}{c^{2}}) + W_{c} (\frac{1}{4} I_{c}^{2} + \frac{1}{1} c^{1} I_{n} + \frac{1}{1} I_{n})^{2}$$

$$I_{y_{tail}} = \frac{W_{t}}{4} (R^{2} + \frac{2}{9} I_{t}^{2}) + W_{t} (\frac{1}{3} I_{t} + I_{n} + I_{c})^{2}$$

$$= \frac{W_{t}}{4} (R^{2} + \frac{2}{9} I_{t}^{2}) + W_{t} (\frac{1}{9} I_{t}^{2} + I_{c}^{2} + I_{n}^{2} + \frac{2}{3} I_{t}I_{c} + \frac{2}{3} I_{t}I_{n}$$

Adding these three together:

$$I_{y} = \frac{R^{2}}{4} (W_{n} + 2W_{c} + W_{t}) + I_{n}^{2} (\frac{W_{n}}{2} + W_{c} + W_{t}) + I_{c}^{2} (\frac{1}{3} W_{c} + W_{t}) + \frac{1}{6} I_{t}^{2} W_{t} + I_{c} I_{n} (W_{c} + 2 W_{t}) + \frac{2}{3} I_{t} I_{c} W_{t} + \frac{2}{3} I_{t} I_{n} W_{t} + W_{s} (Z_{b})^{2}$$
(Roll)

$$I_{x \text{ nose}} = \frac{W_{R}}{2}$$
, $I_{x \text{ cylinder}} = W_{C}R^{2}$, $I_{x \text{ tail}} = \frac{W_{L}R^{2}}{2}$

Adding these three together:

$$I_x = \frac{R^2}{2} (W_n + 2 W_c + W_t) + W_g (Z_b)^2$$

(YAW)

$$I_z = I_{t_4} - W_s (z_b)^2$$

Using the I_{ox} equations for a solid cone and a solid right-cylinder and translating them to the remote axes gives an alternate approach to I_x: $I_x = W_{\underline{p}\underline{c}}R^2 + \frac{3}{10}W_{\underline{p}\underline{n}c}R^2 + (W_{\underline{p}\underline{n}c} + W_{\underline{p}\underline{c}}(Z_{\underline{b}})^2$

7) Internal wing fuel tank centroid

Using the diagram in Section 1 $XFI = \frac{1}{V} \int_{0}^{b} \frac{c+y \tan \Lambda_{L}}{y \tan \Lambda_{L}} \times (t_{L} - \frac{t_{L} + t_{L}}{b}y) dxdy$ $= \frac{1}{V} \int_{0}^{b} (c+y \tan \Lambda_{L})^{2} (t_{L} - \frac{t_{L} + t_{L}}{b}y) - \frac{y^{2} \tan^{2} \Lambda_{L}}{a^{2}} (t_{L} - \frac{t_{L} + t_{L}}{b}y) dy$ $= \frac{b}{V} \left\{ \left[(t_{L} (\frac{c^{2}}{2} + \frac{bc \cdot t \cdot dn}{2} \Lambda_{L} + \frac{b^{2}}{6} (t \cdot dn^{2} \Lambda_{L} - t \cdot dn^{2} \Lambda_{L})) \right] - \left[(t_{L} + t_{L}) (\frac{c^{2}}{a} + \frac{cb \cdot t \cdot dn}{3} \Lambda_{L} + \frac{b^{2}}{6} (t \cdot dn^{2} \Lambda_{L} - t \cdot dn^{2} \Lambda_{L})) \right] \right\}$ YFI is the same as the spanwise centroid for surfaces derived in

section 2. v(volume) was derived in section 2.

(8) Internal fuselage fuel inertia

$$V = \frac{W_{ff}}{\rho}$$

$$R_{f} = \frac{V}{\Pi 1_{f}}$$

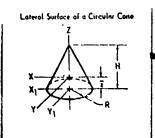
See Section 9 for solid cylinder equation

I is assumed equal to 0.

$$I_{oz} = I_{oy} = \frac{W_{ff}}{12} (3(R_f)^2 + 1_f^2) = \frac{W_{ff}}{12} \frac{(3W_{ff}}{\pi \rho 1_f} + 1_f^2)$$

(9) Center of gravity, inertia and surfac. area of various geometric shapes.

Figure	General Properties	Moment of Inertia
Lateral Cylindrical Shell	Surface Area = 2-RH Centroid = = H/2	$\begin{aligned} I_{x} &= I_{y} = \frac{W}{2} (R^{2} + \frac{H^{2}}{6}) \\ I_{z} &= W_{R}^{2} \\ I_{x_{1}} = I_{y_{1}} = \frac{W}{6} (3R^{2} + 2H^{2}) \end{aligned}$

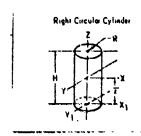


Surface Area =
$$R \sqrt{R^2 + H^2}$$
Controid =
$$\overline{a} = \frac{H}{3}$$

$$i_x = i_y = \frac{W}{4} (R^2 + \frac{2}{9} H^2)$$

$$i_z = \frac{WR^2}{2}$$

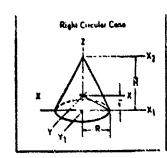
$$i_{x_1} = i_{y_1} = \frac{W}{12} (3R^2 + 2H^2)$$



$$i^{4} = \frac{3}{485}$$

$$i^{4} = i^{3} = \frac{15}{4} (385 + 445)$$

$$i^{4} = i^{3} = \frac{15}{4} (385 + 445)$$



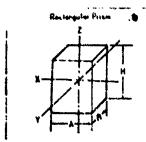
Volume -
$$\frac{dR^2H}{3}$$
Controld -
$$\tilde{\epsilon} = \frac{H}{4}$$

$$i_{m} = i_{y} = \frac{3W}{20} \left(R^{2} + \frac{11^{2}}{4} \right)$$

$$i_{m1} = i_{y1} = \frac{W}{20} \left(3R^{2} + 2H^{2} \right)$$

$$i_{d} = \frac{3W}{10} R^{2}$$

$$i_{m2} = \frac{3W}{20} \left(R^{2} + 4H^{2} \right)$$



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$$t_{B} = \frac{W}{12} (B^{2} + H^{2})$$

$$t_{B} = \frac{W}{12} (A^{2} + H^{2})$$

$$t_{B} = \frac{W}{12} (A^{2} + B^{2})$$